

1

ARITHMETIC

THIS CHAPTER INCLUDES

- Ratios, Variations and Proportion
- Simple and Compound Interest
- Arithmetic Progression and Geometric Progression

OBJECTIVE QUESTIONS

QUESTIONS AND ANSWERS OF JUNE 2013

1. If $x : y = 3 : 4$, $y : z = 5 : 6$ and $z : w = 7 : 8$, then $x : y : z : w$ is
(a) 3:5:7:8 (b) 3:4:6:8
(c) 105: 140: 168: 192 (d) 3 : 4 : 24 : 192 (1 mark)
Answer: (c)
2. The average monthly consumption of petrol for a car for 12 months is 160 litre, if the average monthly consumption for first 8 months is 145 litre, then the average monthly consumption of petrol for the last 4 months is
(a) 190 litre (b) 165 litre
(c) 180 litre (d) 175 litre (1 mark)
Answer: (a)
3. If 9 men working 10 hours daily can complete a job in 10 days, then 15 men working 6 hours daily shall complete same job in
(a) 6 days (b) 8 days
(c) 10 days (d) none of the above (1 mark)
Answer: (c)

4. In 25 years at 8% p.a. simple interest, a sum becomes ₹ 4,629. The amount of sum is
(a) ₹ 1,534 (b) ₹ 1,453
(c) ₹ 1,435 (d) ₹ 1,543 (1 mark)
Answer: (d)
5. A quantity p varies directly as t and another quantity q varies inversely as t . When $t = 2$, $p + q = 1$ and when $t = 3$, $p + q = 8$. When $t = 4$, $p + q =$
(a) 8.5 (b) 9
(c) 9.5 (d) 8 (1 mark)
Answer: (c)

QUESTIONS AND ANSWERS OF SEPTEMBER 2014

1. The monthly salaries of two persons are in the ratio of 3:5. If each receives an increase of ₹ 20 in salary, the ratio is altered to 13:21. Find the respective salaries
(a) ₹ 300, ₹ 500 (b) ₹ 130, ₹ 210
(c) ₹ 240, ₹ 400 (d) ₹ 400, ₹ 240 (1 mark)
Answer: (c)
2. If the two numbers 20 and $x+2$ are in the ratio of 2:3; Find x
(a) 14 (b) 28
(c) 32 (d) 29 (1 mark)
Answer: (b)
3. The simple interest on a sum of money of the end of 8 years is $\frac{2}{5}$ th of the sum itself. Find the rate percent p.a.
(a) 15% (b) 5%
(c) 20% (d) 10% (1 mark)
Answer: (b)
4. In what time will be the S.I. on ₹ 900 at 6% be equal to S.I. on ₹ 540 for 8 years at 5%.
(a) 4 years (b) 10 years
(c) 8 years (d) 6 years (1 mark)
Answer: (a)

5. The fourth term and seventh term of G.P. are 24 and 192 respectively. Find the sum of its first 10 terms.

(a) 2,192 (b) 3,069
(c) 9,063 (d) 192 (1 mark)

Answer: (b)

6. If the sum of first n terms of the series 5, 9, 13, 17,----- is 275, then find n .

(a) $n = 17$ (b) $n = 9$
(c) $n = 11$ (d) $n = 5$ (1 mark)

Answer: (c)

QUESTIONS AND ANSWERS OF DECEMBER 2014

1. What must be subtracted from each of the numbers 17, 25, 31, 47 so that the remainders may be in proportion.

(a) 12 (b) 6
(c) 9 (d) 3 (1 mark)

Answer: (d)

2. The ratios of 200 gm to 2 kg. is:

(a) 100:1 (b) 10:1
(c) 1:1 (d) 1:10 (1 mark)

Answer: (d)

3. If the 5th and 11th terms of an A.P. be 41 and 20, then find its first term and the sum of first 11 terms.

(a) 65, 410.5 (b) 55, 412.5
(c) 50, 412.5 (d) 53, 400.5 (1 mark)

Answer: (b)

4. If a, b, c be the p^{th} , q^{th} and r^{th} term of an A. P. then $a(q - r) + b(r - p) + c(p - q)$ equals:

(a) a (b) 0
(c) b (d) c (1 mark)

Answer: (b)

QUESTIONS AND ANSWERS OF MARCH 2015

1. The Ratio of 5kg 55gm to 35kg 50gm:
(a) 5:7 (b) 1,011:7,010
(c) 111:710 (d) None of these (1 mark)
Answer: (b)
2. If A:B = 3:4, B:C = 2:5 then A:B:C:
(a) 3:4:5 (b) 3:4:10
(c) 4:3:10 (d) 3:4:8 (1 mark)
Answer: (b)
3. Gulshan Kumar borrows ₹ 300 at 5% and ₹ 450 at 6% at the same time and on the condition that the whole loan will be repaid when the total interest amounts to ₹ 126. The loan will have to be repaid after how many years:
(a) 2 (b) 3
(c) 4 (d) 5 (1 mark)
Answer: (b)
4. To find out the total compound interest accrued on a sum of money after 5 years, which of the following information given in the statements P and Q will be sufficient?
P: The sum was ₹ 20,000
Q: The total amount of simple interest on the sum after 5 years was ₹ 4,000.
(a) Only P is sufficient (b) Only Q is sufficient
(c) Either P or Q is sufficient (d) Both P & Q are needed. (1 mark)
Answer: (c)
5. If $\frac{\sqrt{a+\sqrt{b}}}{\sqrt{a-\sqrt{b}}} = \frac{2}{1}$ then $\frac{a+b}{a-b}$ is equal to:
(a) 5/4 (b) 4/5
(c) 3 (d) None of these. (1 mark)
Answer: (a)

QUESTIONS AND ANSWERS OF JUNE 2015

1. If $A : B = 2 : 3$, $B : C = 4 : 5$, then $A : C =$
(a) 6 : 7 (b) 7 : 6
(c) 8 : 15 (d) 15 : 8 (1 mark)
Answer: (c)
2. The ratio of two numbers is 11 : 15. The sum of 3 times the first number and twice the second number is 630. The H.C.F. of the number is:
(a) 10 (b) 12
(c) 15 (d) None of these. (1 mark)
Answer: (a)
3. If $a^{1/3} + b^{1/3} + c^{1/3} = 0$, then $(a + b + c)^3 =$
(a) 3 abc (b) 27 abc
(c) -27 abc (d) None of these. (1 mark)
Answer: (b)
4. The simple interest on ₹ 10 for 4 months at the rate of 3 paise per rupee per month is:
(a) ₹ 1.20 (b) ₹ 12
(c) ₹ 120 (d) ₹ 1200 (1 mark)
Answer: (a)

QUESTIONS AND ANSWERS OF SEPTEMBER 2015

1. A sum of money doubles itself in 10 years. The number of years it would triples itself is
(a) 25 years (b) 15 years
(c) 20 years (d) 10 years (1 mark)
Answer: (c)
2. The fourth proportional of ₹ 5, ₹ 3.50, 150 gm is:
(a) 100 gm (b) 105 gm
(c) 125 gm (d) None of these. (1 mark)
Answer: (b)

3. If $2A = 3B = 4C$, then $A : B : C$ is :
(a) 2 : 3 : 4 (b) 4 : 3 : 2
(c) 6 : 4 : 3 (d) 3 : 4 : 6. (1 mark)
Answer: (c)
4. A person borrowed ₹ 500 at the rate of 5% per annum S.I. what amount will he pay to clear the debt after 4 years?
(a) ₹ 200 (b) ₹ 550
(c) ₹ 600 (d) ₹ 700 (1 mark)
Answer: (c)
5. A sum of money at compound interest amounts to thrice itself in 3 years. In how many years will it be 9 times itself in?
(a) 12 (b) 9
(c) 6 (d) 8 (1 mark)
Answer: (c)
6. If x varies inversely with y and if $y = 3$, then $x = 8$. The value of y when $x = 2$ are :
(a) 24 (b) 18
(c) 12 (d) None of these. (1 mark)
Answer: (c)

QUESTIONS AND ANSWERS OF DECEMBER 2015

1. The C.I. on ₹ 40,000 at 10% p.a. for 1 year when the interest is payable quarterly is:
(a) ₹ 4,000 (b) ₹ 4,100
(c) ₹ 4,15,251 (d) None of these (1 mark)
Answer: (c)
2. If $A:B = 2:3$ $B:C = 4:5$ then $A:C$
(a) 6 : 7 (c) 7 : 6
(c) 8 : 15 (d) 15 : 8 (1 mark)
Answer: (c)

3. The third proportional of 1 hour 20 minutes 1 hour 40 minutes is:
(a) 1 hours 50 minutes (b) 2 hours
(c) 2 hours 5 minutes (d) 2 hours 25 minutes (1 mark)
Answer: (c)
4. If 15% of x is the same as 20% of y, then x : y is
(a) 3 : 4 (b) 4 : 3
(c) 17 : 16 (d) 16 : 17 (1 mark)
Answer: (b)
5. A fraction which bears the same ratio to $\frac{1}{27}$ that $\frac{3}{11}$ does to $\frac{5}{9}$ is:
(a) $\frac{1}{55}$ (b) 55
(c) $\frac{1}{11}$ (d) 14 (1 mark)
Answer: (a)
6. The simple interest on ₹ 10 for 4 months at the rate of 3 paise per rupee per months is:
(a) ₹ 1.20 (b) ₹ 12
(c) ₹ 120 (d) ₹ 1,200 (1 mark)
Answer: (a)
7. To find out the total compound interest accrued on a sum of money after 5 years, which of the following information given in the statements P and Q will be sufficient?
P: The sum was ₹ 20,000.
Q: The total amount of simple interest on the sum after 5 year was ₹ 4,000.
(a) Only P is sufficient (b) Only Q is sufficient
(c) Either P or Q is sufficient (d) Both P & Q is necessary.
(1 mark)
Answer: (d)
8. The fourth term and seventh term of G.P. are 24 and 192 respectively. Find the sum of its first 10 terms.
(a) 2,192 (b) 3,069
(c) 9,063 (d) 192 (1 mark)
Answer: (b)

4.8**Solved Scanner CMA Foundation Paper - 4A (New)**

9. If $x \propto a^2$, then $a \propto \dots\dots\dots$
- (a) x^4 (b) \sqrt{x}
(c) $\frac{1}{\sqrt{x}}$ (d) None of these (1 mark)

Answer: (b)

10. If $x^2 \propto yz$, $y^2 \propto zx$, $z^2 \propto xy$, then the product of three constant of variation is:
- (a) 0 (b) 1
(c) 3 (d) xyz (1 mark)

Answer: (b)**QUESTIONS AND ANSWERS OF MARCH 2016**

1. If $A:B = 2:3$, $B:C = 4:5$, then $A:C =$
- (a) 6:7 (b) 7:6
(c) 8:15 (d) 15:8 (1 mark)

Answer: (c)

2. The inverse ratio of $1\frac{3}{4} : 2\frac{1}{4}$ is_____.
- (a) 32:45 (b) 45:32
(c) 18:5 (d) 5:18 (1 mark)

Answer: (b)

3. The ratio $\frac{5}{3} : 2\frac{1}{4}$ is:
- (a) Ratio of lesser inequality (b) Ratio of greater inequality
(c) 20:9 (d) 5:27 (1 mark)

Answer: (a)

4. The ratio of 5kg. 55gm. to 35kg. 50gm.:
- (a) 5:7 (b) 1,011:7010
(c) 111:710 (d) None of these (1 mark)

Answer: (b)

5. The ratio is 1 year 6 months : 2 years : 2 years 6 months:
(a) 3:4:5 (b) 2:3:5
(c) 2:4:5 (d) None of these (1 mark)
Answer: (a)
6. $\left[\frac{1}{2} + \frac{1}{3}\right] : \left[\frac{1}{2} \times \frac{1}{3}\right]$
(a) 2:3 (b) 3:2
(c) 5:1 (d) 1:5 (1 mark)
Answer: (c)
7. The mean proportional of $4X$ and $16X^3$ is _____.
(a) 10×2 (b) 12×2
(c) 8×2 (d) 64×4 (1 mark)
Answer: (c)
8. If $\frac{1}{5} : \frac{1}{x} = \frac{1}{x} : \frac{1}{1.25}$ the value of x is:
(a) 1.5 (b) 2
(c) 2.5 (d) 3.5 (1 mark)
Answer: (c)
9. If $\frac{a}{3} = \frac{b}{4} = \frac{c}{7}$, then $\frac{a+b+c}{c}$ is equal to:
(a) 7 (b) 2
(c) $\frac{1}{2}$ (d) $\frac{1}{7}$ (1 mark)
Answer: (b)
10. The total number of factors of 210 (excluding 1 and 210) is _____.
(a) 14 (b) 16
(c) 18 (d) 20 (1 mark)
Answer: (a)
11. If $\frac{\sqrt{a+\sqrt{b}}}{\sqrt{a-\sqrt{b}}} = \frac{2}{1}$ then $\frac{a+b}{a-b}$ is equal to:
(a) $5/4$ (b) $4/5$
(c) 3 (d) None of these (1 mark)
Answer: (a)

QUESTIONS AND ANSWERS OF JUNE 2016

1. The fourth proportional of 0.2, 0.12 and 0.3 is:
(a) 0.13 (b) 0.15
(c) 0.18 (d) 0.8 (1 mark)
Answer: (c)
2. The third proportional to $(x^2 - y^2)$ and $(x - y)$ is:
(a) $\frac{x+y}{x-y}$ (b) $\frac{x-y}{x+y}$
(c) $x + y$ (d) $(x - y)$ (1 mark)
Answer: (b)
3. A fraction which bears the same ratio to $\frac{1}{27}$ that $\frac{3}{11}$ does to $\frac{5}{9}$ is:
(a) $\frac{1}{55}$ (b) 55
(c) $\frac{1}{11}$ (d) $\frac{3}{11}$ (1 mark)
Answer: (a)
4. The mean proportional between $\sqrt{11} - \sqrt{5}$ and $13\sqrt{11} + 19\sqrt{5}$ is:
(a) $\sqrt{33} - \sqrt{15}$ (b) $\sqrt{33} + \sqrt{15}$
(c) $\sqrt{11} + \sqrt{5}$ (d) None of these (1 mark)
Answer: (b)
5. A fraction which bears the same ratio to $\frac{1}{27}$ and $\frac{3}{11}$ does to $\frac{5}{9}$ is:
(a) $\frac{1}{55}$ (b) 55
(c) $\frac{1}{11}$ (d) $\frac{3}{11}$ (1 mark)
Answer: (a)

QUESTIONS AND ANSWERS OF DECEMBER 2016

3. Choose the correct answer:

(a) If $\frac{x}{2} = \frac{y}{3}$, then $x : y$ is equal to

- (i) 3 : 2
- (ii) 2 : 3
- (iii) 5 : 6
- (iv) 6 : 5

(1 mark)

Answer: (ii) 2 : 3

(b) If $x \propto y$ and when $x = 5$, $y = 5$ then the value of x when $y = 10$ is

- (i) 100
- (ii) 0
- (iii) 1
- (iv) 10

(1 mark)

Answer: (iv) 10

QUESTIONS OF JUNE 2017

1. Choose the correct answer:

(i) Three numbers are in the ratio 5: 7: 12 and the sum of the first and third numbers is greater than the second by 50. The sum of the three numbers is

- (a) 130
- (b) 120
- (c) 128
- (d) 125

(2 marks)

(ii) In a certain time ₹ 1,400 becomes ₹ 1,848 at 8% p.a. simple interest. When ₹ 2,100 will become ₹ 2,604 at the same time, the rate of interest is

- (a) 8.2%
- (b) 7%
- (c) 10%
- (d) 6%

(2 marks)

- (iii) The year by which a sum of rupees would be 1.21 times of itself at 10% per annum C.I. is
 (a) 2 years (b) 3 years
 (c) 3.5 years (d) 2.5 years **(2 marks)**
- (vi) Which term 128 is, of the progression 1, 2, 4, 8,?
 (a) 8th term (b) 7th term
 (c) 9th term (d) 10th term **(2 marks)**
- (viii) $y = A + B$ where A and B vary directly and inversely respectively with x; $x = 1$ when $y = 11$ and $x = 2$ when $y = 13$. The value of y when $x = 3$ is
 (a) 15 (b) 17
 (c) 19 (d) 20 **(2 marks)**
2. State whether the following statement is True or False:
 (i) $1 + 3 + 5 + 7 + \dots + (2n - 1) = n^2$. **(1 mark)**

PRACTICAL QUESTIONS

2007 - June [1] {C} (a) If the mean proportional between x and 2 is 4, find x. **(1 mark)**

Answer :

4 is the mean proportion of x & 2

$$\text{i.e., } 4 = \sqrt{2x}$$

$$16 = 2x$$

$$x = 8$$

2007 - June [1] {C} (b) The mean of 4 numbers is 9. If one number is excluded the mean becomes 8. Find the excluded number. **(1 mark)**

Answer :

$$\text{We know, } \bar{x} = \frac{\sum x}{n}$$

$$9 = \frac{\sum x}{4}$$

$$\sum x = 36$$

Let the number excluded be x then $\sum x = 36 - x$

$$\bar{x} = \frac{36 - x}{3} = 8$$

$$36 - x = 24$$

$$36 - 24 = x$$

$$x = 12$$

\therefore Excluded number = 12

2007 - June [1] {C} (c) Compute the simple interest on ₹ 5,700 for 2 years at 2.5% p.a. **(1 mark)**

Answer :

$$\text{S.I.} = \frac{P \times n \times i}{100}$$

$$P = ₹ 5700 \quad n = 2 \quad i = \frac{2.5}{100} = 0.025$$

$$\begin{aligned} \text{S.I.} &= 5700 \times 2 \times 0.025 \\ &= ₹ 285 \end{aligned}$$

2007 - June [2] (a) If $\frac{x}{a} = \frac{y}{b} = \frac{z}{c}$, prove that $\frac{x^2 - yz}{a^2 - bc} = \frac{y^2 - zx}{b^2 - ca} = \frac{z^2 - xy}{c^2 - ab}$

(5 marks)

(b) The prime cost of an article was three times the value of the materials used. The cost of raw materials was increased in the ratio 3:4 and the productive wage was increased in the ratio 4:5. Find the present prime cost of an article, which could formerly be made for ₹ 180. **(5 marks)**

Answer :

$$(a) \frac{x}{a} = \frac{y}{b} = \frac{z}{c} = k \text{ (Let)}$$

$$\text{then } x = ak \quad y = bk \quad z = ck$$

$$\frac{x^2 - yz}{a^2 - bc} = \frac{a^2k^2 - bck^2}{a^2 - bc} = 1$$

$$\frac{y^2 - zx}{b^2 - ca} = \frac{b^2k^2 - ack^2}{b^2 - ca} = 1$$

$$\frac{z^2 - xy}{c^2 - ab} = \frac{c^2k^2 - abk^2}{c^2 - ab} = 1$$

$$\therefore \frac{x^2 - yz}{a^2 - bc} = \frac{y^2 - zx}{b^2 - ca} = \frac{z^2 - xy}{c^2 - ab}$$

(b) Let value of material used = x

$$\text{Given prime cost} = ₹, 180$$

$$\text{Prime cost} = 3 \times (\text{value of materials used})$$

$$\text{i.e., } 3x = 180$$

$$\text{or, } x = 60$$

$$\text{value of materials used} = 60$$

$$\therefore \text{material used formerly} = 3x$$

$$\text{or, } 3x = 60$$

$$x = 20$$

$$\text{Similarly labour cost} = 180 - 60$$

$$[\text{prime cost} = \text{value of material used} + \text{labour cost}]$$

$$= 120$$

$$\text{Labour cost formerly} = 4y$$

$$4y = 120$$

$$y = 30$$

$$\text{Present cost of raw material} = 4x$$

$$\text{i.e., } 4 \times 20 = 80$$

$$\text{Similarly cost of Labour} = 5y$$

$$\text{i.e., } 5 \times 30 = 150$$

$$\text{prime cost} = \text{material cost} + \text{labour cost}$$

$$= 80 + 150$$

$$\text{Present prime cost} = ₹ 230$$

2007 - June [3] (a) A dealer of radio offers radio for ₹ 2,720 cash down or for ₹720 cash down and 24 monthly instalments of ₹ 100 each. Find the rate of simple interest charged per annum. **(5 marks)**

Answer :

$$\text{Cash price of radio} = ₹ 2,720$$

$$(-) \text{ down payment} = ₹ 720$$

$$\text{Total installment payment} = ₹ 2,000$$

Each installment of ₹ 100 each is to be cleared in 24 months

let the rate of simple interest to be charged be i

$$2000 (1 + 24i) = 100 (1 + 23i) + 100 (1 + 22i) + \dots + 100 (1 + 0i)$$

$$2000 (1 + 24i) = 100 (24 + i (23 + 22 + \dots + 0))$$

$$2000 (1 + 24i) = 100 (24 + 276i)$$

$$2000 + 48000i = (2400 + 27600i)$$

$$48000i - 27600i = 2400 - 2000$$

$$20400i = 400$$

$$i = \frac{400}{20400} = 0.0196$$

$$\therefore \text{yearly interest rate, } i = 0.0196 \times 12 \\ = 0.2352$$

$$\therefore \text{rate of simple interest charged} = 23.52 \%$$

2007 - June [4] Answer the following :

(d) If $a + b$ varies as $a - b$, prove that $a \propto b$.

(1 mark)

Answer :

Given $a + b$ varies as $a - b$

$$\text{i.e. } \frac{a+b}{a-b} = \text{a constant [As per variation rule]}$$

To prove: a varies as b

$$\text{i.e. } \frac{a}{b} = \text{a constant}$$

$$\text{L.H.S. : } \frac{a+b}{a-b} = k \text{ (let)}$$

$$a + b = ka - kb$$

$$a - ka = -kb - b$$

$$a(1 - k) = -b(k + 1)$$

$$a(k - 1) = b(k + 1)$$

$$a(k - 1) = b(k + 1)$$

$$\frac{a}{b} = \frac{k+1}{k-1} = \text{a constant}$$

∴ L.H.S. = R.H.S.

or $a \propto b$. Hence proved.

2007 - Dec [1] (a) Answer the following :

Choose the correct option showing the proper reason .

(i) If $\frac{2x-3y}{2x+3y} = \frac{2}{5}$ then $x : y$ is

(A) 2 : 7,

(B) 7 : 2,

(C) 2 : 5,

(D) None of these.

(ii) The duplicate ratio of 2 : 3 is

(A) $\sqrt{2} : \sqrt{3}$,

(B) 4 : 6,

(C) 4 : 9,

(D) None of these.

(iii) Compounded ratio of 3 : 7, 21 : 25 is

(A) 25 : 9,

(B) 7 : 21,

(C) 3 : 25,

(D) None of these. **(3 marks each)**

(iv) A person takes loan ₹ 3,000 at 11% per annum from a bank. He repays the loan after 2 years. Then he pays

(A) ₹ 3,300

(B) ₹ 3,660

(C) ₹ 4,000

(D) None of these. **(1 mark)**

Answer :

$$(i) \frac{2x-3y}{2x+3y} = \frac{2}{5}$$

$$10x - 15y = 4x + 6y$$

$$10x - 4x = 6y + 15y$$

$$6x = 21y$$

$$\frac{x}{y} = \frac{21}{6} = \frac{7}{2}$$

∴ Option (B) is correct.

(ii) Duplicate ratio of 2 : 3

$$= 2 \times 2 : 3 \times 3$$

$$= 4 : 9$$

∴ Option (C) is correct.

(iii) Compounded ratio of 3 : 7 & 21 : 25 is

$$3 \times 21 : 7 \times 25$$

$$63 : 175$$

$$\text{Or } 9 : 25$$

∴ Option (D) is correct.

(iv) P = ₹ 3000 r = 11 % n = 2 years

$$\text{Simple interest} = \frac{P \times r \times n}{100}$$

$$= 3000 \times \frac{11}{100} \times 2$$

$$= ₹ 660$$

$$\therefore \text{he repays} = ₹ 3000 + ₹ 660$$

$$= ₹ 3660$$

Option (B) is correct

2007 - Dec [1] (b) Answer the following:

(i) The ages of 5 boys are 5, 8, 10, 13 and 14 years. What is their average age? **(2 marks)**

(iii) If $\frac{\sqrt{x}-\sqrt{y}}{\sqrt{x}+\sqrt{y}} = \frac{1}{2}$, find $\frac{x}{y}$ **(2 marks)**

Answer :

(i) Average age of 5 boys = $\frac{5+8+10+13+14}{5}$

$$= \frac{50}{5} = 10 \text{ Years}$$

4.18 ■ **Solved Scanner CMA Foundation Paper - 4A (New)**

(iii) Given $\sqrt{x} - \sqrt{y} = 1$ and $\sqrt{x} + \sqrt{y} = 2$, by solving both equations

$$\sqrt{x} - \sqrt{y} = 1 \dots\dots\dots (i)$$

$$\sqrt{x} + \sqrt{y} = 2 \dots\dots\dots (ii)$$

$$2\sqrt{x} = 3$$

$$\sqrt{x} = \frac{3}{2}, \quad x = \frac{9}{4}$$

Putting value of \sqrt{x} in eq (i)

$$\frac{3}{2} - \sqrt{y} = 1$$

$$-\sqrt{y} = 1 - \frac{3}{2}$$

$$-\sqrt{y} = -\frac{1}{2}$$

$$\sqrt{y} = \frac{1}{2}$$

$$y = \frac{1}{4}$$

$$\frac{x}{y} = \frac{\frac{9}{4}}{\frac{1}{4}} = \frac{9}{4} \times \frac{4}{1} = 9$$

2007 - Dec [2] Answer the following :

(a) If $\frac{x}{y+z} = \frac{y}{z+x} = \frac{z}{x+y} = K$ prove that $x + y + z = 0$ if $K \neq \frac{1}{2}$ **(4 marks)**

(c) A car travels a distance of 40 km at a speed of 20 km per hour, a second distance of 50 km at a speed of 25 km per hour and a third distance of 210 km at a speed of 35 km per hour. Find the average speed of the car driving the whole distance. **(4 marks)**

Answer :

$$(a) \frac{x}{y+z} = \frac{y}{z+x} = \frac{z}{x+y} = K$$

$$x = (y + z) k$$

$$y = (z + x) k$$

$$z = (x + y) k$$

to prove : $x + y + z \neq 0$ if $k = \frac{1}{2}$

Since, putting value of k in equ (i)

$$x + y + z = \frac{2 \times 1}{2} (x + y + z) = 1$$

Hence proved that $x + y + z = 0$

$$(c) \text{ Average distance Covered} = \frac{40 + 50 + 210}{3}$$

$$= \frac{300}{3} = 100 \text{ km}$$

$$\text{time taken for 1st 40 km} = \frac{40}{20} = 2 \text{ hours}$$

$$\text{time taken for next 50 km} = \frac{50}{25} = 2 \text{ hours}$$

$$\text{time taken for last 210 km} = \frac{210}{35} = 6 \text{ hours}$$

$$\text{average time} = \frac{2+2+6}{3} = 3.3333$$

$$\text{Average speed of the car} = \frac{\text{Avg. distance}}{\text{Avg. time}}$$

$$= \frac{100}{3.3333} = 30 \text{ km / hr.}$$

2007 - Dec [3] (b) Answer the following :

(iii) If a varies as b then show that $a + b$ varies as $a - b$

(1 mark)

Answer :

Given: a varies as b

$$\text{i.e. } \frac{a}{b} = \text{a constant [As per variation rule]}$$

To prove: $a + b$ varies as $a - b$

$$\text{i.e. } \frac{a+b}{a-b} = \text{a constant}$$

$$\text{L.H.S: } \frac{a}{b} = k \text{ (let)}$$

$$a = bk$$

$$\frac{a+b}{a-b} = \frac{bk+b}{bk-b} = \frac{b(k+1)}{b(k-1)} = \text{a constant}$$

$$\therefore \text{L.H.S} = \text{R.H.S}$$

$a + b$ varies as $a - b$

2008 - June [1] (a) Answer the following:

Choose the correct option showing the proper reasons/calculations.

- (i) If x be added to the numbers 10 and 30, then they will be in the ratio 3:4. So x is
 (A) 20 (B) 30
 (C) 50 (D) none of these **(1 mark)**
- (ii) Subtriplicate ratio of 8 : 27 is
 (A) 2 : 3 (B) 512 : 19683
 (C) $2\sqrt{2} : 3\sqrt{3}$ (D) none of these **(1 mark)**
- (iv) The mean of 4 numbers is 10. If one number is excluded the mean will be 8. The excluded number is
 (A) 10 (B) 8
 (C) 9 (D) none of these **(1 mark)**

Answer :

$$(i) \frac{10+x}{30+x} = \frac{3}{4}$$

$$40 + 4x = 90 + 3x$$

$$x = 50$$

\therefore Option (C) is correct.

(ii) Sub triplicate ratio of 8 : 27

$${}^3\sqrt{8} : {}^3\sqrt{27}$$

$$2 : 3$$

∴ Option (A) is correct.

(iv) We know, $\bar{x} = \frac{\sum x}{n}$

$$10 = \frac{\sum x}{4}$$

$$\sum x = 40$$

Let the number exclude be x then $\sum x = 40 - x$

$$\bar{x} = \frac{40-x}{3} = 8$$

$$40 - x = 24$$

$$40 - 24 = x$$

$$x = 16$$

∴ Option (D)

2008 - June [1] (b) Answer the following:

(i) If $\frac{a}{2} = \frac{b}{3} = \frac{c}{4}$ then find the value of $\frac{a+b+c}{b}$ where none of a, b, c is zero.

(2 marks)

(iii) A man mixed 3 litres of kerosene oil, purchased at ₹2 per litre and 2 litres of kerosene oil, purchased at ₹ 4.50 per litre. Find the cost price of the mixture per litre.

(2 marks)

Answer :

(i) $\frac{a}{2} = \frac{b}{3} = \frac{c}{4} = k$ (Let)

$$a = 2k, \quad b = 3k, \quad c = 4k$$

$$\frac{a+b+c}{b} = \frac{2k+3k+4k}{3k} = \frac{9k}{3k} = 3$$

$$\begin{aligned}
 \text{(iii) Cost price of the mixture} &= \frac{3 \times 2 + 2 \times 4.5}{3 + 2} \\
 &= \frac{6 + 9}{5} \\
 &= \frac{15}{5} = ₹ 3 \text{ per litre}
 \end{aligned}$$

2008 - June [2] Answer the following:

- (b) A class has 3 divisions. Average marks of the students of the class, first division, second division and third division are 47, 44, 50 and 45 respectively in Mathematics. If first two divisions have 30 and 40 students, find the number of students in third division when all the students of the class have Mathematics as a subject. **(4 marks)**
- (c) Two vessels contain mixtures of milk and water in the proportion 1:2 and 3:2 respectively. In what proportion should the two mixtures be mixed together so as to form a new mixture containing equal quantity of milk and water ? **(4 marks)**

Answer :

- (b) Let the no. of students in third division be x.

Applying combined mean formula

$$\begin{array}{lll}
 n_1 = 30 & n_2 = 40 & n_3 = x \\
 \bar{x}_1 = 44 & \bar{x}_2 = 50 & \bar{x}_3 = 45 \\
 \bar{x} = 47
 \end{array}$$

$$\begin{aligned}
 \bar{x} &= \frac{n_1 \bar{x}_1 + n_2 \bar{x}_2 + n_3 \bar{x}_3}{n_1 + n_2 + n_3} \\
 47 &= \frac{30 \times 44 + 40 \times 50 + x \times 45}{30 + 40 + x} \\
 47 &= \frac{1320 + 2000 + 45x}{70 + x}
 \end{aligned}$$

$$3290 + 47x = 3320 + 45x$$

$$47x - 45x = 3320 - 3290$$

$$2x = 30$$

$$x = 15$$

∴ No. of students in third division = 15

(c) Let x litre is drawn form vessel 1 and y litre form vessel 2

$$\frac{\frac{x}{3} + \frac{3y}{5}}{\frac{2x}{3} + \frac{2y}{5}} = \frac{1}{1}$$

$$\frac{x}{3} + \frac{3y}{5} = \frac{2x}{3} + \frac{2y}{5}$$

$$\frac{3y}{5} - \frac{2y}{5} = \frac{2x}{3} - \frac{x}{3}$$

$$\frac{y}{5} = \frac{x}{3}$$

$$\frac{x}{y} = \frac{3}{5}$$

∴ the proportion of two mixture = 3 : 5.

2008 - June [4] Answer the following :

(c) The monthly expenses of a boarding house are partly fixed and partly varied with the number of boarders. The monthly charges are ₹ 100 per head when there are 25 boarders and ₹ 80 per head when there are 15 boarders. If the monthly charge per head is ₹ 70 find the number of boarders. **(4 marks)**

Answer :

Let total cost function for boarders be $y = a + bx$

Where y = cost

x = no. of boarders

and a and b are constants.

According to Question

$$25 \times 100 = a + 25b \text{ ----- (i)}$$

$$80 \times 15 = a + 15b \text{ ----- (ii)}$$

Solving eq(i) and (ii) simultaneously

$$a + 25b = 2500$$

$$a + 15b = 1200$$

$$\begin{array}{r} (-) \quad (-) \quad (-) \\ \hline \end{array}$$

$$10b = 1300$$

$$b = 130$$

Putting value of b in eq(i)

$$a + 25 \times 130 = 2500$$

$$a = 2500 - 3250$$

$$a = -750$$

$$\therefore \text{Total cost function} = -750 + 130x$$

If the monthly charge per head is ₹70, then number of boarders

$$= 70x = -750 + 130x$$

$$70x - 130x = -750$$

$$-60x = -750$$

$$x = \frac{750}{60} = 12.5$$

$$\therefore \text{Number of boarders} = 12.5$$

Number of boarders can't be in fraction. Hence correct answer is 12.

2008 - Dec [1] Answer the following :

Choose the correct option showing the proper reasons/calculations.

(a) Two numbers are in the ratio 3 : 4. If 10 is subtracted from both of them the ratio will be 1 : 2. So the numbers are

(A) 15 and 20, (B) 12 and 16, (C) 30 and 40, (D) None of them.

(2 marks)

(b) The mean of age of 5 men is 40 years. Three of them are of same age and they are excluded. The mean of the remaining two is 25. Age of one of the excluded persons in years is

(A) 20, (B) 25, (C) 40, (D) None of them.

(2 marks)

(c) A man bought three qualities of tea in the ratio 5 : 4 : 3 with prices per kg. ₹ 390, ₹ 375 and ₹ 450 respectively and mixed them together. The cost price of the mixture per kg. in ₹ is

(A) 395, (B) 420, (C) 400, (D) None of them.

(2 marks)

(d) Ram lends Hari ₹ 1,000 and Hari repays ₹ 1,300 to Ram at the end of 3 years in simple interest fully. The rate of interest Ram charged to Hari per annum for repayment of loan is

(A) 13%, (B) 12%, (C) 10%, (D) None of them.

(2 marks)

Answer :

(a) Let the numbers are $3x$ and $4x$

Now,

$$\frac{3x-10}{4x-10} = \frac{1}{2} \rightarrow 6x-20=4x-10$$

$$\Rightarrow 2x = 10$$

$$\Rightarrow x = 5$$

Hence number are $3 \times 5 = 15$

$$\text{and } 4 \times 5 = 20$$

\therefore option (A) is correct.

(b) Let the age of 5 men are

x, x, x, y and z

Now, Given

$$\frac{x+x+x+y+z}{5} = 40$$

$$3x + y + z = 200 \dots\dots\dots(i)$$

$$\text{Again Given } \frac{y+z}{2} = 25$$

$$y + z = 50 \dots\dots\dots(ii)$$

Putting value of eqn. (ii) in eqn. (i) we get

$$3x + 50 = 200$$

$$3x = 150$$

$$x = 50 \text{ years}$$

\therefore Age of one of excluded persons in years is 50 years.

\therefore Option (D) is correct.

(c) Cost price of the mixture per kg. in ₹ is

$$\frac{5 \times 390 + 4 \times 375 + 3 \times 450}{5 + 4 + 3}$$

$$= \frac{1,950 + 1,500 + 1,350}{12}$$

$$= \frac{4,800}{12} = ₹ 400 \text{ per kg}$$

\therefore Option (C) is correct.

4.26**Solved Scanner CMA Foundation Paper - 4A (New)****(d)** Given $P = 1000$

$$A = 1300$$

$$t = 3 \text{ years}$$

$$S.I = A - P$$

$$\text{Or } \frac{Prt}{100} = 1300 - 1000$$

$$\frac{1000 \times r \times 3}{100} = 300$$

$$r = 10\%$$

 \therefore Option (C) is correct.**2008 - Dec [2]** Answer the following :

(a) The proportion of liquid I and liquid II in four samples are 2 : 1, 3 : 2, 5 : 3 and 7 : 5. A mixture is prepared by taking equal quantities of the four samples. Find the ratio of liquid I to liquid II in the final mixture.

(4 marks)**Answer :**

$$\frac{\text{liquid I}}{\text{liquid II}} = \frac{\frac{2}{3}x + \frac{3}{5}x + \frac{5}{8}x + \frac{7}{12}x}{\frac{1}{3}x + \frac{2}{5}x + \frac{3}{8}x + \frac{5}{12}x}$$

$$\frac{80 + 72 + 75 + 70}{40 + 48 + 45 + 50} = \frac{297}{183} = \frac{99}{61}$$

 \therefore ratio of liquid I to liquid II in final mixture is 99 : 61**2008 - Dec [3]** (a) Answer the following :

(ii) If $y \propto \frac{1}{x^3}$ and $x = 2$ when $y = 3$, then for $x = 3$ the value of y is

(A) $\frac{4}{3}$, (B) $\frac{8}{9}$, (C) $\frac{4}{9}$, (D) None of them.

(2 marks)**Answer :**

$$y \propto \frac{1}{x^3} \text{ and } x = 2 \text{ when } y = 3$$

$$\text{When } y \propto \frac{1}{x^3}$$

$$y = k \frac{1}{x^3} \text{ (where } k \text{ is a constant)}$$

when $x = 2$ and $y = 3$

$$= k \cdot \frac{1}{2^3} = k = 24$$

$$\therefore \text{when } x = 3 \text{ then } y = 24 \times \frac{1}{3^3} = \frac{24}{27} = \frac{8}{9}$$

\therefore Option (B) is correct.

2008 - Dec [4] Answer the following :

- (c) The volume of a gas varies directly as the absolute temperature and inversely as pressure. When the pressure is 10 units and the temperature is 200 units, the volume is 160 units. What will be the volume when pressure is 12 units and temperature is 480 units ?

(3 marks)

Answer :

Let, V = Volume, T = temperature (absolute), P = pressure

$$\text{Then, } V \propto \frac{T}{P} \text{ i.e., } V = \frac{KT}{P}, K = \text{constant.}$$

$$\text{For } P = 10 \text{ unit, } T = 200 \text{ unit, } V = 160 \text{ unit, } 160 = \frac{200K}{10}$$

$$\text{or, } K = \frac{1600}{200} \text{ or, } K = 8 \text{ i.e., } V = \frac{8T}{P}$$

$$\text{Hence, required volume (V)} = \frac{8 \times 480}{12} = 8 \times 40 = 320 \text{ cubic units.}$$

2009 - June [1] Answer the following:

Choose the correct option showing the proper reasons/calculations.

- (a) Let marks obtained by Ram, Rahim and Jadu be A , B , and C respectively. Given $A : B = 1:2$, $B:C = 3:4$. The combined ratio $A : B : C$ is

- (i) $1 : 2 : 4$,
- (ii) $3 : 6 : 8$,
- (iii) $1 : 6 : 8$,
- (iv) None of them.

(3 marks)

(b) If $\frac{\sqrt{a}+\sqrt{b}}{\sqrt{a}-\sqrt{b}} = \frac{2}{1}$ then $\frac{a+b}{a-b}$ is equal to

- (i) 5/4
- (ii) 4/5
- (iii) 3
- (iv) None of them

(3 marks)**Answer :**

(a) If $A : B = 1 : 2$ and $B : C = 3 : 4$

$$\begin{aligned} \text{Then } A:B:C &= 1 \times 3 : 2 \times 3 : 2 \times 4 \\ &= 3 : 6 : 8 \end{aligned}$$

(b) $\frac{\sqrt{a}+\sqrt{b}}{\sqrt{a}-\sqrt{b}} = \frac{2}{1}$

Using componendo and Dividendo.

$$\frac{\sqrt{a}+\sqrt{b}+(\sqrt{a}-\sqrt{b})}{\sqrt{a}-\sqrt{b}-(\sqrt{a}-\sqrt{b})} = \frac{2+1}{2-1}$$

$$\frac{2\sqrt{a}}{2\sqrt{b}} = \frac{3}{1}$$

Squaring both sides, we get

$$\frac{a}{b} = \frac{9}{1}$$

using again componends and Dividendo

$$\frac{a+b}{a-b} = \frac{10}{8} = \frac{5}{4}$$

2009 - June [2] Answer the following :

(a) If $\frac{x}{b+c} = \frac{y}{c+a} = \frac{z}{a+b}$ then show that $(b-c)(x-a) + (c-a)(y-b) +$

$$(a-b)(z-c) = 0.$$

(4 marks)

(b) A person borrowed ₹ 10,000 at some simple interest rate for 2 years. After expiry of one year he borrowed another ₹ 20,000 at 1% lower interest rate for 1 year. At the end he paid fully ₹ 33,000. Find the rate of interest at which he borrowed first.

(4 marks)

Answer :

$$(a) \frac{x}{b+c} = \frac{y}{c+a} = \frac{z}{a+b} = k \text{ (let)}$$

$$\therefore x = k(b+c)$$

$$y = k(c+a)$$

$$z = k(a+b)$$

Now,

L.H.S.

$$= (b-c)(x-a) + (c-a)(y-b) + (a-b)(z-c)$$

$$= (b-c)\{k(b+c)-a\} + (c-a)\{k(c+a)-b\} + (a-b)k(a+b)-c\}$$

$$= k(b^2 - c^2) - (ab - ac) + k(c^2 - a^2) - (bc - ab) + k(a^2 - b^2) - (ac - bc)$$

$$= k(b^2 - c^2 + c^2 - a^2 + a^2 - b^2) - (ab - ac + bc - ab + ac - bc)$$

$$= 0$$

= R.H.S.

(b) Let r be the required rate of interest

$$P = ₹ 10,000$$

Simple Intt. for 2 year on ₹ 10,000 at $r\%$ intt.

$$= \frac{10,000 \times r \times 2}{100} = 200r$$

Since after one year he borrowed another 20,000 hence principle is ₹ 30,000 and at $(r-1)\%$ intt. rate

$$= \frac{20,000 \times (r-1) \times 1}{100} = 200(r-1)$$

Total interest received in 2 years = 33,000 - 30,000 = ₹ 3,000

$$\therefore 200r + 200(r-1) = 3,000$$

$$200r + 200r - 200 = 3,000$$

$$400r = 3200 = r = \frac{3,200}{400} = 8\%$$

2009 - June [4] Answer the following :

(b) The total expenses of a boarding house varies partly with the number of boarders and partly fixed. The total expenses are ₹ 10,000 for 25 boarders and ₹ 11,500 for 30 boarders. Find the fixed expenses.

(3 marks)

4.30**Solved Scanner CMA Foundation Paper - 4A (New)****Answer :**

Let the expenses be x
& variable expenses by y

$$\therefore x + 25y = 10,000 \quad \text{..... (1)}$$

$$x + 30y = 11,500 \quad \text{..... (2)}$$

- - -

$$5y = 1,500$$

$$y = 300$$

Putting the value of y in eq. (i)

$$x + 25 \times 300 = 10,000$$

$$\text{or, } x = 10,000 - 7,500$$

$$\therefore x = 2,500$$

$$\therefore \text{Fixed expenses} = 2,500$$

$$\text{Variable exp. per boarder} = 300$$

2009 - Dec [1] Answer the following:

Choose the correct option showing the proper reasons/calculations.

(a) The number to be added to each term of the ratio 3 : 7 to make it 1 : 2 is

(i) 2,

(ii) 1,

(iii) 3,

(iv) None of these.

(3 marks)

(b) The average of 7 numbers is 27. If one number is included, the average becomes 25. The included number is

(i) 11,

(ii) 10,

(iii) 12,

(iv) None of these.

(3 marks)

(c) The time in which a sum of money becomes double at 10% p.a., simple interest is

(i) 8 years,

(ii) 10 years,

(iii) 12 years,

(iv) None of these.

(3 marks)

Answer :

(a) Let the number added is x.

$$\text{Now } \frac{3+x}{7+x} = \frac{1}{2}$$

$$\text{or } 6 + 2x = 7 + x$$

$$\text{or } x = 1 \quad \text{Option (ii)}$$

(b) Let the number included is x

Given averages of seven number = 27

$$\frac{\sum x}{7} = 27$$

$$\text{or } \sum x = 7 \times 27 \\ = 189$$

i.e. Total of Seven numbers = 189

$$\text{Again Given } \frac{189+x}{8} = 25$$

$$\text{or } 189 + x = 200$$

$$\text{or } x = 11 \quad \text{Option (i)}$$

(c) Let the sum of money = P

and hence Amount = 2P

$$\text{Now } A = P \left(1 + \frac{rt}{100} \right)$$

$$\text{or, } 2p = P \left(1 + \frac{10.t}{100} \right)$$

$$\text{or, } 2 = 1 + \frac{10t}{100}$$

$$\text{or, } 2 = 1 + \frac{t}{10}$$

$$\text{or, } t = 10 \text{ years} \quad \text{Option (ii)}$$

4.32**Solved Scanner CMA Foundation Paper - 4A (New)****2009 - Dec [2]** Answer the following:

- (b) In a liquid mixture 20% is water and in another mixture water is 25%. These two mixtures are mixed in the ratio 5 : 3. Find the percentage of water in the final mixture. **(4 marks)**

Answer :

Let in first liquid ratio of water to others = 20% : 80%
= 1 : 4

$$\text{Proportion of water} = \frac{x}{5}$$

Similarly, in second liquid, ratio of water and others = 25% : 75% = 1:3

$$\therefore \text{Proportion of water} = \frac{y}{4}$$

$$\text{Now given } \frac{\frac{x}{5}}{\frac{y}{4}} = \frac{5}{3}$$

$$\frac{4x}{5y} = \frac{5}{3}$$

$$\frac{x}{y} = \frac{25}{12}$$

$$\therefore x : y = 25 : 12$$

2009 - Dec [3] Answer the following:

Choose the correct option showing necessary reasons/ calculations.

- (c) Given a varies as $bx + c$. Value of a is 3 when $b = 1$, $c = 2$ and is 5 when $b = 2$, $c = 3$. The value of x would be
(i) -1, (ii) 2. (iii) 3. (iv) none of these. **(3 marks)**

Answer :Given a varies as $bx + c$

i.e. $a = k(bx + c)$ where $k = a$ Constant
when $b = 1$ and $c = 2$ then $a = 3$

$$3 = k(x + 2) \quad \text{----- (i)}$$

When $b = 2$ and $c = 3$ then $a = 5$

$$5 = k(2x + 3) \quad \text{----- (ii)}$$

Divide eqn (1) by (ii) we get

$$\frac{K(x+2)}{K(2x+3)} = \frac{3}{5}$$

$$5x + 10 = 6x + 9$$

$$x = 1 \quad \text{option (iv)}$$

2010 - June [1] Answer the following:

Choose the correct option showing the proper reasons/calculations.

(a) If x is the mean proportional between $x - 2$ and $x + 6$ then the value of x is

- (i) 4
- (ii) 3
- (iii) 2
- (iv) None of these

(3 marks)

(b) Of the five numbers the average of first four numbers is 8 and the average of the last four numbers is 6. Then the difference of the first and the fifth number is

- (i) 6
- (ii) 8
- (iii) 10
- (iv) None of these

(3 marks)

Answer :

(a) Given $\frac{x-2}{x} = \frac{x}{x+6}$

$$x^2 = (x - 2)(x + 6)$$

$$x^2 = x^2 + 6x - 2x - 12$$

$$4x - 12 = 0$$

$$4x = 12$$

$$x = 3 \quad \text{option (ii)}$$

(b) Let the five numbers are $x_1, x_2, x_3, x_4,$ & x_5

$$\text{Given } \frac{x_1 + x_2 + x_3 + x_4}{4} = 8 \quad \Rightarrow \quad x_1 + x_2 + x_3 + x_4 = 32$$

$$\Rightarrow \quad x_2 + x_3 + x_4 = 32 - x_1 \quad \text{---- (i)}$$

4.34**Solved Scanner CMA Foundation Paper - 4A (New)**

$$\text{and } \frac{x_2 + x_3 + x_4 + x_5}{4} = 6 \quad \Rightarrow \quad x_2 + x_3 + x_4 + x_5 = 24$$

$$\Rightarrow \quad x_2 + x_3 + x_4 = 24 - x_5 \quad \text{---- (ii)}$$

Solving (i) & (ii)

$$32 - x_1 = 24 - x_5$$

$$x_1 - x_5 = 32 - 24$$

$$= 8 \quad \text{option (ii)}$$

2010 - June [2] Answer the following:

(a) Divide ₹ 6,200 in 3 parts such that the interest for the three parts for 2, 3 and 5 years respectively at 5% simple interest p.a. are same.

(4 marks)

(b) A dealer mixes two varieties of teas costing ₹ 100 per kg. and ₹160 per kg. in the proportion 5:1. He sold the 6 kg. mixture at the rate of ₹ 120 per kg. Find his profit.

(4 marks)**Answer :**

(a) 1st part is x, 2nd part is y, 3rd part is z

$$\therefore x + y + z = 6,200$$

$$\text{Interest on 1}^{\text{st}} \text{ part} = x \times \frac{5}{100} \times 2 = \frac{x}{10}$$

$$\text{Interest on 2}^{\text{st}} \text{ part} = y \times \frac{5}{100} \times 3 = \frac{3y}{20}$$

$$\text{Interest on 3}^{\text{st}} \text{ part} = z \times \frac{5}{100} \times 5 = \frac{z}{4}$$

$$\therefore \frac{x}{10} = \frac{3y}{20} = \frac{z}{4} = K$$

$$\therefore x = 10K, y = \frac{20K}{3}, z = 4K$$

$$\therefore 10K + \frac{20K}{3} + 4K = 6,200 \Rightarrow K = 300$$

$$1^{\text{st}} \text{ part} = 10 \times 300 = 3,000, 2^{\text{nd}} \text{ part} = 20 \times \frac{300}{3} = 2,000, 3^{\text{rd}} \text{ part} = 4,300$$

$$= 1,200$$

(b) Let us calculate the cost of mixture by Urery formula of weighted avg.

$$\therefore \text{Cost of mixture} = \frac{5 \times 100 + 1 \times 160}{5 + 1} = ₹ 110$$

$$\therefore \text{Cost of 6 kg mixture} = ₹ 6 \times 110 = ₹ 660$$

$$\text{and selling price of 6 kg mixture} = ₹ 6 \times 120 = ₹ 720$$

$$\begin{aligned} \therefore \text{Profit} &= 720 - 660 \\ &= ₹ 60 \end{aligned}$$

2010 - June [3] Answer the following:

(e) The area of a circle varies directly with square of its diameter. Area of the circle is 38.5 sq.cm when diameter is 7 cm. If diameter of the circle is 1 cm then area of the circle in sq.cm is

(i) 5.5/7 (ii) 11/7 (iii) 22/7 (iv) None of these

(3 marks)

Answer :

Let the area of circle = A

diameter of the circle = d

Given $A \propto d^2$

or $A = k \cdot d^2$ [where k is a constant]

Given A = 38.5 sq.cm and d = 7 cm

$$\therefore A = k \cdot d^2$$

$$38.5 = k \cdot 7^2$$

$$\text{or } k = \frac{5.5}{7}$$

Again when d = 1cm and $k = \frac{5.5}{7}$ cm

$$\text{Then } A = \frac{5.5}{7} \times 1^2 = \frac{5.5}{7} \text{ sq. cm } \quad \text{option (i)}$$

2010 - June [4] Answer the following:

(c) The volume of a gas varies directly as the absolute temperature and inversely as pressure. When the pressure is 15 units and the temperature is 260 units the volume is 200 units. What will be the volume when the pressure is 18 units and the temperature is 195 units?

(3 marks)

4.36**Solved Scanner CMA Foundation Paper - 4A (New)****Answer :**Let volume = V Pressure = P and Absolute Temperature = T Given $V \propto T$ and $V \propto \frac{1}{P}$ or $V = K \frac{T}{P}$ where $K = \text{Constant}$ When $P = 15$, $T = 260$ then $V = 200$

$$200 = K \frac{260}{15} \Rightarrow K = \frac{150}{13}$$

Hence, when $P = 15$ and $T = 260$

$$\text{Then, } V = \frac{150}{13} \times \frac{195}{18} = 125 \text{ units}$$

2010 - Dec [1] Answer the following :

Choose the correct option showing the proper reasons/ calculations :

(a) If $P = \frac{4}{5}Q$ and $Q = 2\frac{1}{2}R$, then $P : R$ is

(i) 1 : 2

(ii) 2 : 1

(iii) 4 : 5

(iv) none of these

(3 marks)

(b) A person drove his car 40 km at an average speed of 20 km per hour and next 60 km at an average speed of 30 km per hour. Then his average speed in his whole journey of 100 km is

(i) 25 km/h

(ii) 20 km/h

(iii) 30 km/h

(iv) none of these

(3 marks)

(c) Time in which ₹ 5,000 will be the amount ₹ 6,000 at simple interest @ 5% p.a. is

(i) 2 years

(ii) 5 years

(iii) 4 years

(iv) none of these

(3 marks)

Answer :

$$(a) \frac{P}{R} = \frac{P}{Q} \times \frac{Q}{R} = \frac{4}{5} \times \frac{5}{2} = \frac{2}{1} = P : R = 2 : 1 \text{ Ans, (ii)}$$

(b) Whole distance covered = 40 + 60 = 100 km

$$\text{Time taken} = \frac{40}{20} + \frac{60}{30} = 4 \text{ hrs.}$$

$$\text{So average speed in whole distance} = \frac{\text{distance}}{\text{time}} = \frac{100}{4}$$

$$= 25 \text{ km/hr} \quad \text{Ans. (i)}$$

(c) Given Time = t years , rate (r) = 5%

$$\text{Principal (p)} = ₹ 5,000$$

$$\text{Amount (A)} = ₹ 6,000$$

Hence Simple Interest = A – P

$$= ₹ 6,000 - ₹ 5,000 = ₹ 1,000$$

$$\text{Now time} = \frac{\text{S.I} \times 100}{p \times r} = \frac{1,000 \times 100}{5,000 \times 5} = 4 \text{ years option (iii)}$$

2010 - Dec [2] Answer the following :

(a) A dealer mixed two varieties of tea having cost ₹ 1,200 and ₹ 2,500 per kg each in such a way that he can gain 20% by selling the resultant mixture at ₹ 1,800 per kg. Find the proportion in which the two types of teas are mixed. **(4 marks)**

Answer :

Let the proportion of two types of teas are x_1 & x_2 and cost price of mixture

$$= \frac{100}{120} \times 1800 = ₹ 1,500 \text{ hence we can write}$$

$$1,500 = \frac{1200x_1 + 2500x_2}{x_1 + x_2}$$

$$1500(x_1 + x_2) = 1200x_1 + 2500x_2$$

$$1500x_1 + 1500x_2 = 1200x_1 + 2500x_2$$

$$300x_1 = 1000x_2$$

$$\frac{x_1}{x_2} = \frac{10}{3}$$

Hence required proportion is 10:3

4.38**Solved Scanner CMA Foundation Paper - 4A (New)****2010 - Dec [4]** Answer the following :

- (a) The expense of a boarding house are partly fixed and partly varies with the number of boarders. The charge is ₹ 70 per head when there are 20 boarders and ₹ 60 per head when there are 40 boarders. Find the charge per head when there are 50 boarders. **(3 marks)**

Answer :

$$\text{Let } Y = a + bx \quad \text{----- (i)}$$

Where $x = \text{No. of boarders}$
and $y = \text{charges per head.}$

$$\text{If } x = 20, Y = 70$$

$$\text{from (1) } \quad 70 = a + 20b \quad \text{----- (ii)}$$

$$\text{again } x = 40 y = 60$$

$$\text{from (1) } 60 = a + 40b \quad \text{----- (iii)}$$

Solving (ii) & (iii) we get

$$a + 20b = 70$$

$$a + 40b = 60$$

$$- 20b = 10$$

$$b = -1/2$$

$$\therefore a = 80$$

$$\therefore \text{Hence from (i) } y = 80 - \frac{1}{2}x$$

$$\text{If } x = 50$$

$$\text{They } Y = 80 - \frac{1}{2} \times 50 = 55$$

2011 - June [1] Answer the following :

Chose the correct option showing the proper reasons/calculations.

- (a) If $2 -x, 3 -x, 5 -x$ and $7 -x$ are in proportion, then the value of x is

(i) 1,

(ii) -1,

(iii) 2,

(iv) None of these.

(3 marks)

- (b) The average of 10 numbers is 21. If an additional number is included the average becomes 20. The additional number is
- (i) 10,
 - (ii) 5,
 - (iii) 3,
 - (iv) None of these.
- (3 marks)**

Answer :

- (a) \therefore The given expression are in proportion.
 \therefore The product of extreme terms = product of middle terms
 $\therefore (2 - x)(7 - x) = (3 - x)(5 - x)$
 $\therefore 14 - 2x - 7x + x^2 = 15 - 3x - 5x + x^2$
 $\therefore 14 - 15 = -8x + 9x$
 $-1 = x$
 $\therefore x = -1$ **Option (ii)**

- (b) The average of 10 numbers = 21
 \therefore Total = $10 \times 21 = 210$
 Let the Additional number be x
 \therefore Total + x = Average \times Total no
 $\therefore 210 + x = 20 \times 11$
 $210 + x = 220$
 $\Rightarrow x = 10$ **Option (i)**

2011 - June [2] Answer the following :

- (a) Due to fall in rate of interest from 12% to 10% per annum in 4 years, home loan amount of a person decreases by ₹ 4,800. Find the home loan he took first. **(4 marks)**
- (b) At what ratio sugar at ₹ 30 per kg be mixed with sugar at ₹ 35 per kg to produce a mixture making profit 25% when sold at ₹ 40 per kg ? **(4 marks)**

Answer :

- (a) P = Home loan the person took first
 n yrs = time period, i_1 = first rate of interest, i_2 = second rate of interest
 Then $4800 = (P + Pn i_1) - (P + Pn i_2) = Pn(i_1 - i_2) = P \cdot 4 (12/100 - 10/100)$
 i.e. $P = ₹ 60,000$.

4.40**Solved Scanner CMA Foundation Paper - 4A (New)**

(b) $X = 30 \text{ ₹/kg}$
 $Y = 35 \text{ ₹/kg}$
Profit % = 25%
Selling price = 40 ₹/kg
Let Cost Price be = x

$$x + \frac{25}{100}x = 50$$
$$x = \frac{40 \times 100}{125} = 32 \text{ ₹/kg.}$$
$$x \times 30 + y \times 35 = (x + y) \times 32$$
$$30x + 35y = 32x + 32y$$
$$3y = 2x$$
$$\frac{3}{2} = \frac{x}{y}$$
$$3 : 2$$

2011 - June [3] Answer the following :

- (c) If c varies directly as $x + b$, $c = 8$ when $b = 2$ and $c = 10$ when $b = 3$ then value of x is
- (i) 0,
 - (ii) 1,
 - (iii) 2,
 - (iv) None of these.

(3 marks)

Answer :

$$c \propto (x + b) \text{ i.e., } c = k(x + b), k \neq 0$$

$$\text{Thus } 8 = k(x + 2) \text{ and } 10 = k(x + 3)$$

$$\text{i.e. } \frac{8}{10} = \frac{x+2}{x+3} \Rightarrow x = 2 \text{ option (iii)}$$

2011 - Dec [1] Answer the following:

Choose the correct option showing the proper reasons/calculations.

- (a) Two numbers are in the ratio of 3 : 4. If 10 is subtracted from both of them then the ratio becomes 1 : 3. The numbers are
- (i) 9 and 12
 - (ii) 12 and 16
 - (iii) 15 and 20
 - (iv) None of these

(3 marks)

- (b) A person drove his car 50 km at an average speed of 20 km/h. He drove first 30 km of his journey at an average speed of 60 km/h. Then average speed of last 20 km is
- 40 km/h
 - 25 km/h
 - 10 km/h
 - None of these
- (3 marks)**
- (c) For a sum of money to become $2\frac{1}{4}$ times of itself in 5 years, the rate of interest is
- 25%
 - 30%
 - 35%
 - None of these
- (3 marks)**

Answer :

- (a) Let the number be x

\therefore According to the question.

$$\frac{3x - 10}{4x - 10} = \frac{1}{3}$$

$$\Rightarrow 9x - 30 = 4x - 10$$

$$\Rightarrow 9x - 4x = -10 + 30$$

$$5x = 20$$

$$x = 4$$

\therefore the ratio will be, $3x : 4x = 3 \times 4 : 4 \times 4 = 12 : 16$ **Option (ii)**

- (b) Total distance = 50 km

Average speed = 20 km/hr

$$\therefore \text{Total time taken} = \frac{\text{Total distance}}{\text{Average Speed}}$$

$$= \frac{50 \text{ km} \times \text{hr}}{20 \text{ km}} = \frac{5 \text{ hr}}{2} = 2.5 \text{ hr}$$

1st Journey covered distance = 30 km

Average speed = 60 km/hr

$$\text{Time taken} = \frac{30 \text{ km} \times \text{hr}}{60 \text{ km}}$$

$$= \frac{1}{2} \text{ hr}$$

4.42**Solved Scanner CMA Foundation Paper - 4A (New)**

$$\therefore \text{Now Rest time} = \frac{5}{2} \text{ hr} - \frac{1}{2} \text{ hr} = 2 \text{ hr}$$

Now again Rest distance = 20 km

$$\text{Time} = 2 \text{ hr}$$

$$\therefore \text{Average speed} = \frac{\text{Total distance}}{\text{Total time}} = \frac{20 \text{ km}}{2 \text{ hr}} = 10 \text{ km/hr} \quad \text{Option (iii)}$$

(c) Let the Principal be x

$$\therefore \text{Amount will be} = \frac{9}{4} x$$

time = 5 years

Since we know that

$$P = \frac{A}{1 + rt}$$

$$x = \frac{\frac{9}{4}x}{1 + 5r}$$

$$\Rightarrow 1 + 5r = \frac{9}{4}$$

$$5r = \frac{9}{4} - 1$$

$$5r = \frac{9 - 4}{4}$$

$$5r = \frac{5}{4}$$

$$r = \frac{1}{4}$$

$$\therefore \text{rate} = \frac{1}{4} \times 100 = 25\% \quad \text{Option (i)}$$

2011 - Dec [2] Answer the following:

(a) If $\frac{\alpha}{q-r} = \frac{\beta}{r-p} = \frac{\gamma}{p-q}$ then prove that $\alpha + \beta + \gamma = 0 = p + q + r$.

(4 marks)

Answer :

$$\frac{\alpha}{q-r} = \frac{\beta}{r-p} = \frac{\gamma}{p-q} = k \text{ (let)}$$

$$= k(q-r) \dots\dots(i) = k(r-p) \dots\dots(ii) \gamma = k(p-q) \dots\dots(iii)$$

Adding (i), (ii) & (iii)

$$+ \quad + \quad \gamma = k(q-r) + k(r-p) + k(p-q)$$

$$= kq - kr + kr - pk + pk - kq$$

$$+ \quad + \quad \gamma = 0$$

Hence proved

Again

$$p + q + r\gamma = pk(q-r) + qk(r-p) + rk(q-p)$$

$$= kpq - pkr + kqr - kqp + prk - rqk$$

$$p + q + r\gamma = 0$$

Hence proved.

2011 - Dec [3] Answer the following:

Choose the correct option showing proper reasons/calculations.

(c) Let $A - k$ varies directly as B where k is constant. If $A = 750$ then $B = 500$. If $A = 1,175$ then $B = 1,350$. If $A = 550$ then B will be

- (i) 100
- (ii) 200
- (iii) 250
- (iv) None of these

(3 marks)

Answer :

$$A - k \propto B$$

$$A - k = Bt \quad (t \text{ is a constant})$$

$$750 - k = 500t$$

$$(-) 1175 - k = 1350t$$

$$(+) \quad (-)$$

$$- 425 \quad = \quad - 850t$$

$$t = \frac{1}{2}$$

If $A = 550$, then, $550 - 500 = B/2$

$$B = 100 \quad \text{option (i)}$$

2012 - June [1] Answer the following :

Choose the correct option showing the proper reasons/calculations.

(a) 10 years before, the ages of father and son were in the ratio 5:2. If at present their total age is 90 years, the present age of the son is

- (i) 40 years
- (ii) 25 years
- (iii) 30 years
- (iv) None of these

(3 marks)

(b) If the speed of a car to go uphill is 20 km/hr and down is 30 km/hr, then average speed of the car is (in km/hr)

- (i) 23
- (ii) 24
- (iii) 25
- (iv) None of these

(3 marks)

Answer :

(a) Let the father's present age = x
And son's present age = y

Given, $\frac{x-10}{y-10} = \frac{5}{2}$

Or, $2x - 20 = 5y - 50$

Or, $2x - 5y = -30$ (i)

And $x + y = 90$ (given)(ii)

Solving equation (i) and (ii), we get,

$x = 60$

$y = 30$

Therefore, the present age of son is 30 yrs. **Option (iii)**

(b) Average speed is calculated with the help of Harmonic mean (H.M.).

Therefore, Average Speed = $\frac{2}{\frac{1}{20} + \frac{1}{30}} = 24$ km/hr **Option (ii)**

2012 - June [2] Answer the following :

(a) Two vessels contain mixtures of milk and water in the ratio 5:1 and 9:1. They are mixed together in the ratio 1:5. Find the ratio of milk and water in the final mixture.

(4 marks)

- (b) An amount of money at certain rate of simple interest per annum becomes ₹ 2,400 in 4 years and ₹ 2,500 in 5 years. Find the rate of interest p.a. **(4 marks)**

Answer:

- (a) Let 1 litre of mixture of first vessel be mixed with 5 Litres of mixture of second vessel.

1 Litre of first vessel contains $1 \times \frac{5}{6} = \frac{5}{6}$ litre of milk and $1 \times \frac{1}{6} = \frac{1}{6}$ litre of

water.

5 Litre of second vessel contains $5 \times \frac{9}{10} = \frac{9}{2}$ litre of milk and $5 \times \frac{1}{10} = \frac{1}{2}$

litre of water.

So, in the final mixture, milk : water = $\left(\frac{5}{6} + \frac{9}{2}\right) : \left(\frac{1}{6} + \frac{1}{2}\right) = 8 : 1$

- (b) Let P be the initial sum invested

Given A = 2,400 in 4 years

Therefore, $A = P \left(1 + \frac{rt}{100}\right)$

$$2,400 = P \left(1 + \frac{4r}{100}\right) \dots\dots\dots(i)$$

Again, Given, A = 2,500 in 5 years

Therefore, $2,500 = P \left(1 + \frac{5r}{100}\right) \dots\dots\dots(ii)$

Dividing (i) by (ii)

$$\frac{2,400}{2,500} = \frac{P(1+0.04r)}{P(1+0.05r)}$$

$$\frac{24}{25} = \frac{1+0.04r}{1+0.05r}$$

$$24 + 1.20r = 25 + r$$

$$0.2r = 1$$

$$r = \frac{1}{0.2} = 5\% \text{ p.a.}$$

4.46**Solved Scanner CMA Foundation Paper - 4A (New)****2012 - June [3]** Answer the following :

Choose the correct option showing proper reasons/calculations.

(b) If $(a + b) \propto (a - b)$ and when $a = 6$, $b = 2$, then for $b = 3$, the value of a is

- (i) 6
- (ii) 9
- (iii) 12
- (iv) none of these

(3 marks)**Answer:**Since $(a + b) \propto (a - b)$ Therefore, $a + b = k(a - b)$

$$\frac{a+b}{a-b} = \frac{k}{1}$$

by applying, componendo & dividendo rule,

$$\frac{a+b+a-b}{a+b-a+b} = \frac{k+1}{k-1}$$

$$\frac{2a}{2b} = \frac{k+1}{k-1}$$

$$\frac{a}{b} = \frac{k+1}{k-1}$$

for $a = 6$, $b = 2$

$$\frac{6}{2} = \frac{k+1}{k-1}$$

Therefore, $k = 2$ Therefore, for $b = 3$, and $k = 2$

$$\frac{a}{3} = \frac{2+1}{2-1}$$

 $a = 9$ **Option (ii)****2012 - June [4]** Answer the following :

(c) The total expenses of a boarding house are partly fixed and the rest varies as the number of boarders. The charges is ₹ 100 per head when there are 25 boarders and ₹ 80 when there are 50 boarders. Find the number of boarders for which the total expense will be ₹ 7000.

(3 marks)

Answer:

Fixed Cost = C_1 , Total Cost = C , No. of boarders = n

Therefore, $C = C_1 + kn$

Hence, $2,500 = C_1 + 25k$ and $4,000 = C_1 + 50k$

$C_1 = 1,000$, $k = 60$

Therefore $C = 1,000 + 60n$

Therefore, When $C = 7,000$, $n = 100$.

The no. of boarders is 100.

Alternative solution

Variable cost per unit =

$$\frac{\text{Change in total cost}}{\text{Change in units}} = \frac{(50 \times 80) - (25 \times 100)}{(50 - 25)} = \frac{(4,000 - 2,500)}{25}$$

= 60 per boarder

Fixed Cost per unit = Total Cost - Variable Cost

= $4,000 - (50 \times 60) = 1,000$

If Total Cost = 7,000 therefore total Variable Cost = 6,000

No. of boarders = $\frac{6,000}{60} = 100$ boarders

2012 - Dec [1] Answer the following:

Choose the correct option showing the proper reasons/calculations.

(a) The average of 4 numbers is 13. If one number is excluded the average becomes 15. The excluded number is

(i) 5

(ii) 6

(iii) 7

(iv) none of these.

(3 marks)

(b) The compound ratio of $x : 2$, $2 : 3$ and $3 : y$ is

(i) $y : x$

(ii) $x : y$

(iii) $2 : 5$

(iv) none of these.

(3 marks)

4.48**Solved Scanner CMA Foundation Paper - 4A (New)**

- (c) A sum of ₹ 1,200 amounts to ₹ 1,536 in 2 years at simple interest. The rate of interest per annum is
- (i) 14%
 - (ii) 12%
 - (iii) 11%
 - (iv) none of these.
- (3 marks)**

Answer :

- (a) (iii) Excluded number = $(4 \times 13) - (3 \times 15) = 7$
- (b) (ii) The compound ratio $x \times 2 \times 3 : 2 \times 3 \times y = x : y$
- (c) (i) $\frac{1200 \times R \times 2}{100} = 1536 - 1200$
 $24R = 336$
 $R = 14 \quad \therefore R = \text{Rate of Interest} = 14 \%$

2012 - Dec [2] Answer the following:

- (b) A number is added to each of the numbers 7,15,21 and 37 so that the resulting numbers are in proportion. Find the number added. **(4 marks)**

Answer :

Let the number to added be x.

$$\frac{7+x}{15+x} = \frac{21+x}{37+x}$$

$$\text{or, } (21 + x)(15 + x) = (37 + x)(7 + x)$$

$$\text{or, } 315 + 21x + 15x + x^2 = 259 + 37x + 7x + x^2$$

$$\text{or, } 36x + x^2 - 44x - x^2 = 259 - 315$$

$$\text{or, } -8x = -56$$

$$\text{or, } x = 7$$

 \therefore 7 will be added each of the numbers.**2012 - Dec [3]** Answer the following:

Choose the correct option showing proper reasons/calculations.

- (e) Given $A = B + C$, when $B = x^2$ and $C = x^3$. If $A = 0$ when $x = 1$ and $A = 2$ when $x = -1$, then A in terms of x is
- (i) $2x^2 - x^3$
 - (ii) $x^2 - 2x^3$
 - (iii) $x^2 - x^3$
 - (iv) none of these.
- (3 marks)**

Answer :

$$A = B + C = k_1 x^2 + k_2 x^3 \text{ [assuming } B = k_1 x^2 \text{ \& } C = k_2 x^3]$$

$$A = 0, x = 1 \Rightarrow k_1 + k_2 = 0 \text{ and } A = 2, x = 1 \Rightarrow k_1 - k_2 = 2$$

Hence, solving the above two $k_1 = 1$ and $k_2 = -1$,

$$\text{So } A = B + C = x^2 - x^3.$$

2016 - Dec [1] Answer the questions:

- (a) A sum of money invested at compound interest amounts to ₹ 10,816 at the end of second year and to ₹ 11,248.64 at the end of third year, find the rate of interest.
- (c) Two numbers are in the ratio of 2 : 7 and if 9 be added to each of them, the sums become in the ratio 1 : 2. Find the numbers.

(5 × 2 = 10 marks)

Answer:

$$(a) \quad A = P \left(1 + \frac{C}{100} \right)^n$$

$$10,816 = P \left(1 + \frac{C}{100} \right)^2 \text{ _____ (1)}$$

$$11,248.64 = P \left(1 + \frac{C}{100} \right)^3 \text{ _____ (2)}$$

Dividing (2) by (1) we have,

$$\frac{11,248.64}{10,816} = \left(1 + \frac{C}{100} \right)$$

$$\frac{C}{100} = \frac{11,248.64}{10,816} - 1$$

$$\frac{C}{100} = \frac{432.64}{10,816}$$

$$C = 4\%.$$

- (c) Let the two numbers be $2x$ and $7x$

Then, $2x + 9 : 7x + 9 = 1 : 2$

$$\text{or } \frac{2x+9}{7x+9} = \frac{1}{2}$$

Cross multiplying, we get ,

$$4x + 18 = 7x + 9$$

$$7x - 4x = 18 - 9$$

$$\text{or } 3x = 9$$

$$\therefore x = 3$$

Hence, the two numbers are (2×3) and (7×3)

i.e. 6 and 21

2016 - Dec [2] Answer the questions:

(a) A man deposits ₹ 10,000 at the end of each year in a bank which pays 5% p.a. compound interest. If the installments are allowed to accumulate, what will be the total accumulation at the end of 10 years? (Given $(1.05)^{10} = 1.62889$ (approximately)).

(c) Find the ratio of ${}^5P_2 : {}^5C_2$.

(3 × 2 = 6 marks)

Answer:

$$\begin{aligned} \text{(a) Future Value} &= 10,000 \left[\frac{(1 + 0.05)^{10} - 1}{0.05} \right] \\ &= 10,000 \left[\frac{(1.05)^{10} - 1}{0.05} \right] \\ &= 10,000 \left[\frac{1.62889 - 1}{0.05} \right] \\ &= \frac{10,000 \times 0.62889}{0.05} \\ &= ₹ 1,25,778 \end{aligned}$$

$$\begin{aligned} \text{(c) } {}^5P_2 : {}^5C_2 &= \frac{{}^5P_2}{{}^5C_2} \\ &= \frac{\frac{n!}{(n-r)!}}{\frac{n!}{(n-r)!r!}} = r! = 2! = 2 \end{aligned}$$

2016 - Dec [7] (d) A sum of ₹ 10,000 is invested for simple interest at the rate of 10% per annum for 3 years. Find the amount received as interest after 3 years.

(1 mark)

Answer:

$$\text{Interest} = 10,000 \times \frac{10}{100} \times 3 = ₹ 3,000$$

2017 - June [3] Answer the questions:

(b) If – 15, – 25 are respectively the 11th and 16th terms of an A.P., then find the sum of first 20 terms of the A.P. (4 marks)

(d) Find the sum of n terms of the series 2 + 22 + 222 + (4 marks)

TOPIC NOT YET ASKED BUT EQUALLY IMPORTANT FOR EXAMINATION

PRACTICAL QUESTIONS

Q.1 While on vacation Priya's diesel purchases were: 10 litres @ ₹ 35.5; 10 litres @ ₹ 36.9; 8 litres @ ₹ 37.5; 14 litres @ ₹ 34. What average price per litre did she pay for the diesel?

Answer :

Purchases in Litres	Rate (₹)	Total Expenditure (₹)
(1)	(2)	(3) = (2) × (1)
10	35.5	355
10	36.9	369
8	37.5	300
<u>14</u>	<u>34</u>	<u>476</u>
42		1,500

$$\text{Average price per litre of diesel} = \frac{1500}{42} = ₹ 35.71$$

Q.2 A man invested his savings as follows:

₹ 10,000 in Post Office Savings Bank at 8% p.a.

₹ 6,000 in a National Bank at 7% p.a.

₹ 4,000 in a Private Firm at 10% p.a.

Find the average rate of interest per cent p.a.

Answer :

Investment	Amount ₹	Rate of return %	Return ₹
	(1)	(2)	(3) = (1) × (2)
Post office	10,000	8	800
National Bank	6,000	7	420
Private Firm	<u>4,000</u>	10	<u>400</u>
	20,000		1,620

$$\text{Average rate of interest in \%} = \frac{1,620 \times 100}{20,000} = 8.10\%$$

4.52**Solved Scanner CMA Foundation Paper - 4A (New)**

Q.3 Speed of a car to go up a hill is 10 km per hour and to go down is 20 km per hour. Compute its average speed.

Answer :

Here in the above situation, HM is the appropriate mean.

$$\begin{aligned} \text{Average speed} &= \frac{2}{\frac{1}{10} + \frac{1}{20}} \\ &= \frac{2}{0.1 + 0.05} \\ &= \frac{2}{0.15} = 13.333 = 13\frac{1}{3}. \end{aligned}$$

Q.4 In a firm out of 1200 employees 650 are males and rest are females. Average monthly wages of males is ₹ 4,500 and of females is ₹ 5,000. Find the average wage paid by the firm.

Answer :

Sex	No. of employees	Average monthly wages (₹ in)	Total wages paid (₹ in)
Male	(1) 650	(2) 4,500	(3) = (2) × (1) 29,25,000
Female	<u>550</u> 1,200	5,000	<u>27,50,000</u> 56,75,000

$$\text{Average wage paid by the firm} = \frac{56,75,000}{1,200}$$

$$\begin{aligned} &= 4,729.17 \text{ (approx)} \\ &₹ 4,729.17 \text{ approx.} \end{aligned}$$

Q.5 X, Y, Z are three children. Y was born when X was 4 years 7 months old and Z was born when Y was 3 years 4 months old. Find their average age when Z was 5 years 2 months old.

Answer :

Person	Age in year	Age in month
X	4 Years 7 months	4 × 12 + 7 = 55
Y	3 years 4 months	3 × 12 + 4 = 40
Z	5 years 2 months	5 × 12 + 2 = 62

We have to find average age when z was 5 years 2 months old

∴ Y's age at this moment = 40 + 62 = 102

Similarly X's age at this moment = 55 + 40 + 62 = 157

∴ Average age in month = $\frac{102 + 157 + 62}{3} = 107$

and Average age in year = 8 years 11 months

Q.6 The mean of 3 numbers is 15. With inclusion of a fourth number, the mean becomes 17. Find the included number.

Answer :

We know $\bar{x} = \frac{\sum x}{n}$

$$15 = \frac{\sum x}{3}$$

$$\sum x = 15 \times 3 = 45$$

Let the fourth number include be x

$$\text{New mean} = \frac{45+x}{4}$$

$$17 = \text{New mean} = \frac{45+x}{4}$$

$$45 + x = 68$$

$$X = 68 - 45$$

$$= 23$$

∴ included number = 23.

Q.7 Monthly rainfall from June to September of a certain year was 12.5 cm, 27.04 cm, 20.05 cm and 6.29 cm respectively. Find the average daily rainfall during these four months.

Answer :

Monthly Rainfall in cm no. of days in respective month

Month	Rainfall in c.m.	No. of days in respective month
June	12.5	30
July	27.04	31
August	20.05	31
September	6.29	30
	<u>65.88</u>	<u>122</u>

4.54**Solved Scanner CMA Foundation Paper - 4A (New)**

$$\text{Average days} = \frac{122}{4} = 30.5$$

$$\text{Average rainfall in month} = \frac{65.88}{4} = 16.47$$

$$\begin{aligned} \therefore \text{Average daily rainfall during these four month} \\ = \frac{16.47}{30.5} = 0.54 \text{ cm.} \end{aligned}$$

Q.8 A person drove his car for 20 km. at an average speed of 25 km. per hour. At what average speed must he drive for the next 20 km., if his average speed for the whole distance is to be 30 km. per hour?

Answer :

$$\text{Time taken for 1}^{\text{st}} \text{ 20 Km} = \frac{20}{25} = 0.8$$

$$\text{let average speed for next 20 km be } x \text{ then, time taken for next 20 km} = \frac{20}{x}$$

$$\text{Average time} = \frac{0.8 + \frac{20}{x}}{2}$$

$$\text{Average distance} = \frac{20+20}{2} = \frac{40}{2} = 20$$

$$\text{Average speed} = \frac{\text{Averagedistance}}{\text{Averagetime}}$$

$$30 = \frac{20}{\frac{0.8 + \frac{20}{x}}{2}}$$

$$30 = \frac{40}{0.8 + \frac{20}{x}}$$

on cross multiplication

$$4 = 2.4 + \frac{60}{x}$$

$$4x = 2.4x + 60$$

$$4x - 2.4x = 60$$

$$1.6x = 60$$

$$x = \frac{60}{1.6} = 37.5 \text{ km/hr.}$$

Q.9 An employer pays wages ₹ 60 per male worker and ₹ 45 per female worker each per day. If he engages 8 male and 4 female workers on some day then find the average wage per worker on that day.

Answer :

Sex	No. of employees	Wages per worker (in ₹)	Total wages paid (in ₹)
	(1)	(2)	(3) = (2) x (1)
Male	8	60	480
Female	4	45	180
	<u>12</u>		<u>660</u>

$$\text{Average wage per worker} = \frac{660}{12} = ₹ 55$$

Q.10 A person drove his car for first 20 km and then 30 km at an average speed of 20 km and 30 km per hour respectively. At what speed must he drive next 50 km if the average speed of the whole distance of his driving is 40 km per hour ?

Answer :

$$\text{Average distance} = \frac{20+30+50}{3} = 33.333 \text{ km}$$

$$\text{time taken for 1}^{\text{st}} \text{ 20 km} = \frac{20}{20} = 1$$

$$\text{time taken for next 30 km} = \frac{30}{30} = 1$$

$$\text{Let speed for next 50 km} = x \text{ km/hr}$$

$$\text{time taken for last 50 km} = \frac{50}{x}$$

4.56**Solved Scanner CMA Foundation Paper - 4A (New)**

$$\begin{aligned} \text{Average time taken} &= \frac{1+1+\frac{50}{x}}{3} \\ &= \frac{2+\frac{50}{x}}{3} \end{aligned}$$

$$\begin{aligned} \text{Average speed} &= \frac{\text{Average distance}}{\text{Average time}} \\ &= \frac{33.333}{\frac{2+\frac{50}{x}}{3}} \\ 40 &= \frac{99.999}{2+\frac{50}{x}} \end{aligned}$$

on cross multiplication

$$\begin{aligned} 80 + \frac{2000}{x} &= 99.999 \\ 80x + 2000 &= 99.999x \\ 2000 &= 19.999x \\ x &= 100 \end{aligned}$$

Average speed is 100 km. per hour.

Q.11 The average score of boys is 60, that of girls is 70 and that of all the candidates is 64 appearing in Mathematics of annual examination. Find the ratio of number of boys and number of girls there. If the total number of candidates appearing in Mathematics is 150, find the number of boys there.

Answer :Let no. of boys be x , then no. of girls $150 - x$

$$\text{now, } n_1 = x, \quad n_2 = 150 - x$$

$$\bar{x}_1 = 60 \quad \bar{x}_2 = 70$$

$$\bar{x} = 64$$

using combined mean formula

$$\bar{x} = \frac{n_1 \bar{x}_1 + n_2 \bar{x}_2}{n_1 + n_2}$$

$$64 = \frac{x \times 60 + (150 - x) \times 70}{150}$$

$$64 \times 150 = 60x + 10500 - 70x$$

$$9600 = 10500 - 10x$$

$$-900 = -10x$$

$$x = \frac{900}{10}$$

$$= 90$$

∴ Number of boys = 90

Number of boys (n) = 90.

Q.12 If $16p = 25q$, find the duplicate ratio of p to q.

Answer :

$$16p = 25q$$

$$\frac{p}{q} = \frac{25}{16}$$

Duplicate ratio of p & q

$$\frac{p^2}{q^2} = \frac{25^2}{16^2} = \frac{625}{256}$$

Q.13 The volume of a gas varies as the absolute temperature and inversely as the pressure. When the pressure is 15 units and the temperature is 260 (in absolute units) the volume is 200 cc What will be the volume when the pressure is 18 units and the temperature is 390 (in absolute units)?

Answer:

$$V = \frac{K \times T}{P}$$

Where

- V = Volume of gas
- K = Pressure
- T = Temperature
- P = Some arbitrary constant

4.58**Solved Scanner CMA Foundation Paper - 4A (New)**

$$\text{Given } P = 15$$

$$T = 260$$

$$V = 200$$

$$200 = \frac{K \times 260}{15}$$

$$K = \frac{200 \times 15}{260}$$

$$\text{Volume, when } T = 390 \text{ } P = 18$$

$$V = \frac{200 \times 15}{260} \times \frac{390}{18} = 250 \text{ cc}$$

Q.14 If $\frac{5a+3b}{4a+5b} = \frac{2}{3}$ find the ratio of a : b

Answer :

$$\frac{5a+3b}{4a+5b} = \frac{2}{3}$$

$$3(5a+3b) = 2(4a+5b)$$

$$15a+9b = 8a+10b$$

$$15a-8a = 10b-9b$$

$$7a = b$$

$$\frac{a}{b} = \frac{1}{7}$$

$$\therefore a : b = 1 : 7$$

Q.15 Find the ratio compounded of the duplicate ratio of 2x: 3y and ratio 27y²: 8x³.

Answer :

$$\begin{aligned} \text{Duplicate ratio of } 2x : 3y &= 2x \times 2x : 3y \times 3y \\ &= 4x^2 : 9y^2 \end{aligned}$$

$$\begin{aligned} \text{Compound ratio} &= 4x^2 \times 27y^2 : 9y^2 \times 8x^3 \\ &= 108 x^2 y^2 : 72y^2 x^3 \end{aligned}$$

Note : This can be further reduced to $\frac{108x^2y^2}{72y^2x^3}$

Q.16 Two mixtures contain milk and water in the ratio of 7:2 and 5:1. In what ratio these two mixtures should be mixed so that the resulting mixture may contain milk and water in the ratio 9:2?

Answer :

Milk	7
Water	2

I

Milk	5
Water	1

II

Let x litre is drawn from mixture I and y litre from mixture II.
Then ratio of milk and water in mixture II.

$$\frac{\frac{7x}{9} + \frac{5y}{6}}{\frac{2x}{9} + \frac{y}{6}} = \frac{9}{2}$$

$$\frac{14x}{9} + \frac{10y}{6} = \frac{18x}{9} + \frac{9y}{6}$$

$$\frac{10y}{6} - \frac{9y}{6} = \frac{18x}{9} - \frac{14x}{9}$$

$$\frac{y}{6} = \frac{4x}{9}$$

$$9y = 24x$$

$$\frac{y}{x} = \frac{24}{9}$$

the ratio in which these mixture should be mixed = 24 : 9.

Q.17 The ratio of present age of father to that of his son is 5: 3. Ten years before the ratio was 2 : 1. Find the present ages.

Answer :

Given the ratio of present ages = 5 : 3 & their ratio 10 years before = 2 : 1
this data can also be presented as follows:

Person	Present Age	10 Years before age
Father	5x	5x - 10
Son	3x	3x - 10

$$\therefore \frac{5x-10}{3x-10} = \frac{2}{1}$$

[on cross multiplication]

$$5x - 10 = 6x - 20$$

$$-10 + 20 = 6x - 5x$$

$$x = 10$$

\(\therefore\) present age of father is 50 years and, present age of son is 30 years.

Q.18 If x_1, x_2, \dots, x_n , be in continued proportion, show that $\frac{x_1}{x_n} = \left(\frac{x_1}{x_2}\right)^{n-1}$.

Answer :

$$\text{Let } \frac{x_1}{x_2} = \frac{x_2}{x_3} = \dots = \frac{x_{n-1}}{x_n} = K$$

Multiplying each ratio

$$\text{L.H.S. } \frac{x_1}{x_2} \times \frac{x_2}{x_3} \times \dots \times \frac{x_{n-1}}{x_n} = K^{n-1}$$

$$\therefore \frac{x_1}{x_2} = K^{n-1}$$

$$\text{R.H.S. } \frac{x_1}{x_2} = K, \quad \therefore \left(\frac{x_1}{x_2}\right)^{n-1} = K^{n-1}$$

$$\frac{x_1}{x_n} = \left(\frac{x_1}{x_2}\right)^{n-1}$$

Hence, proved.

Q.19 There are four containers of milk and water in the ratio 2 : 1, 3 : 2, 5 : 3 and 7 : 5. A mixture is prepared with equal quantities drawn from the four containers. Find the ratio of milk to water in the final mixture.

Answer :

Let x litre of milk and water is drawn from each container then the ratio of milk of water in final mixture.

$$\Rightarrow \frac{\frac{2}{3}x + \frac{3}{5}x + \frac{5}{8}x + \frac{7}{12}x}{\frac{x}{3} + \frac{2x}{5} + \frac{3x}{8} + \frac{5x}{12}}$$

$$\Rightarrow \frac{x \left(\frac{2}{3} + \frac{3}{5} + \frac{5}{8} + \frac{7}{12} \right)}{x \left(\frac{1}{3} + \frac{2}{5} + \frac{3}{8} + \frac{5}{12} \right)}$$

Taking L.C.M.,

$$\Rightarrow \frac{\frac{80+72+75+70}{120}}{\frac{40+48+45+50}{120}}$$

$$\Rightarrow \frac{297}{120} \times \frac{120}{183}$$

$$\Rightarrow \frac{297}{183} = 99 : 61$$

Q.20 The expenses of a hotel are partly fixed and the rest varies as the number of boarders. When the number of boarders are 450, the expense is ₹ 1,800 and when the number of boarders in 920, the expenses is ₹ 3,210. Find the expenses per head when there are 100 boarders.

Answer :

Let the linear equation be

$$y = a + bx \text{eq. (a)}$$

Where, x = no. of boarders

y = expenses

a = Fixed expense

b = constant multiplier

$$1,800 = a + 450 b \text{(i)}$$

$$3,210 = a + 920 b \text{(ii)}$$

4.62**Solved Scanner CMA Foundation Paper - 4A (New)**

Solving equation (i) & eq. (ii) we get,

$$a + 450 b = 1,800$$

$$a + 920 b = 3,210$$

$$\begin{array}{r} (-) \quad (-) \quad = \quad (-) \\ \hline \end{array}$$

$$-470 b = -1,410$$

$$b = 3$$

putting value of b in eq (i)

$$a + 450 \times 3 = 1800$$

$$a = 1,800 - 1,350$$

$$a = 450$$

Substituting value of a, b in eq (a)

$$Y = 450 + 3x$$

Where these are 100 boarders, expense =

$$y = 450 + 3 \times 100 = 750$$

$$\text{expenses per head} = \frac{750}{100} = ₹ 7.5$$

Q.21 Monthly incomes of two persons Ram and Rahim are in the ratio 5:7 and their monthly expenditures are in the ratio 7:11. If each of them saves ₹ 60, per month, determine their monthly incomes.

Answer :

Let monthly income of Ram = 5x

Monthly income of Rahim = 7x

Ram's monthly income = ₹ 5x

$$\text{Less : Savings} = \frac{60}{}$$

$$\text{Expenditure} \quad 5x - 60$$

again, Rahim's monthly income = ₹ 7x

$$\text{Less : Savings} = \frac{60}{}$$

$$\text{Expenditure} \quad 7x - 60$$

Ratio of their expenditure = 7 : 11

$$\frac{5x-60}{7x-60} = \frac{7}{11}$$

$$\frac{5x-60}{7x-60} = \frac{7}{11}$$

$$55x - 660 = 49x - 420$$

$$55x - 49x = -420 + 660$$

$$6x = 240$$

$$x = 40$$

$$\begin{aligned}
 \text{Ram's monthly income} &= ₹ 5x \\
 &= 5 \times 40 \\
 &= ₹ 200 \\
 \text{Rahim's monthly income} &= ₹ 7x \\
 &= ₹ 7 \times 40 \\
 &= ₹ 280
 \end{aligned}$$

Q.22 The ratio of the present age of a father to that of his son is 5 : 3. After Ten years hence the ratio would be 3 : 2. Find their present ages.

Answer :

Present age	10 years after age
Let the age of Father be $5x$	$5x + 10$
and that of Son be $3x$	$3x + 10$

$$\frac{5x+10}{3x+10} = \frac{3}{2}$$

[On cross multiplication]

$$10x + 20 = 9x + 30$$

$$10x - 9x = 30 - 20$$

$$x = 10$$

$$\text{Present age of father} = 5x = 5 \times 10 = 50 \text{ years}$$

$$\text{Present age of son} = 3x = 3 \times 10 = 30 \text{ years}$$

Father 50 years, Son 30 years.

Q.23 A dealer mixes tea costing ₹ 8 per kg with tea costing ₹ 7 per kg and thereafter, sells the mixture at ₹ 8 per kg and earns a profit of 7.5% on his sale price. In what proportion does he mix them?

Answer :

$$\text{Let S.P. be } 100$$

$$\text{Less :- Profit } \underline{7.5}$$

$$\text{C.P. } 92.5$$

Let proportion of mixture be $x : y$

$$(8x + 7y) \times \frac{100}{92.5} = 8(x + y)$$

[On cross multiplication]

$$(8x + 7y) = 7.4x + 7.4y$$

$$8x - 7.4x = 7.4y - 7y$$

$$0.6x = 0.4y$$

$$\frac{x}{y} = \frac{0.4}{0.6} = \frac{4}{6} = \frac{2}{3}$$

Q.24 The work done by $n-1$ persons in $n+1$ days is to the work done by $n+1$ persons in $n+2$ days be in the ratio of 5 : 6; find 'n'.

Answer :

$$\frac{(n-1)(n+1)}{(n+1)(n+2)} = \frac{5}{6}$$

$$\frac{n^2-1}{n^2+2n+2} = \frac{5}{6}$$

$$\frac{n^2-1}{n^2+3n+2} = \frac{5}{6}$$

$$6n^2 - 6 = 5n^2 + 15n + 10$$

$$n^2 = 15n + 16$$

$$n^2 - 15n - 16 = 0$$

$$n^2 - 16n + n - 16 = 0$$

$$n(n-16) + 1(n-16) = 0$$

$$n = 16$$

Q.25 Two vessels contain mixtures of milk and water in the proportion 2 : 3 and 4 : 3 respectively. In what proportions should the two mixtures be mixed so as to form a new mixture containing equal quantities of milk and water?

Answer :

Let x litre be drawn from container 1 and y litre be drawn from container 2

$$\frac{\frac{2}{5}x + \frac{4}{7}y}{\frac{3}{5}x + \frac{3}{7}y} = \frac{1}{1}$$

$$\frac{2}{5}x + \frac{4}{7}y = \frac{3}{5}x + \frac{3}{7}y$$

$$\frac{4}{7}y - \frac{3}{7}y = \frac{3}{5}x - \frac{2}{5}x$$

$$\frac{y}{7} = \frac{x}{5}$$

$$5y = 7x$$

$$\frac{x}{y} = \frac{5}{7}$$

The proportion of mixture = 5 : 7.

Q.26 The ratio of the present age of mother to her daughter is 5 : 3. Ten years hence the ratio would be 3 : 2. Find their present ages.

Answer :

Let their present ages be

Person	present age	10 years after age
Mother	5x	5x + 10
Daughter	3x	3x + 10

$$\frac{5x+10}{3x+10} = \frac{3}{2}$$

$$10x + 20 = 9x + 30$$

$$x = 10$$

∴ Present age of mother = 5x
 = 5 × 10
 = 50 years

Present age of daughter = 3x
 = 3 × 10
 = 30 years

Q.27 Find a mean proportional between 27 and 243.

Answer :

If a, b, c can be in proportion then $\frac{a}{b} = \frac{b}{c}$ then b is said to be in the mean proportion, hence $b^2 = ac$

$$\begin{aligned} \text{Mean proportion (b)} &= \sqrt{27 \times 243} \\ &= \sqrt{6561} \\ &= 81 \end{aligned}$$

4.66**Solved Scanner CMA Foundation Paper - 4A (New)**

Q.28 Monthly incomes of two persons are in the ratio 2 : 3 and their monthly expenditures are in the ratio 4 : 7. If each saves ₹ 50 a month, find their monthly incomes and expenditures.

Answer :

Let monthly income be

Person	Income	Saving	Expenditure
1	2x	50	2x - 50
2	3x	50	3x - 50

$$\frac{2x-50}{3x-50} = \frac{4}{7}$$

[On cross multiplication]

$$14x - 350 = 12x - 200$$

$$14x - 12x = -200 + 350$$

$$2x = 150$$

$$x = 75$$

Person	Income	Expenditure
1	2x, 2 × 75 = 150	2x - 50, 2 × 75 - 50 = 100
2	3x, 3 × 75 = 225	3x - 50, 3 × 75 - 50 = 175

Q.29 If $\frac{4x-3z}{4c} = \frac{4z-3y}{3b} = \frac{4y-3x}{2a}$, show that each ratio is equal to

$$\frac{x+y+z}{2a+3b+4c}$$

Answer :

Adding each ratio $\frac{4x-3z+4z-3y+4y-3x}{4c+3b+2a}$

$$= \frac{x+y+z}{4c+3b+2a}, \text{ Proved}$$

Q.30 The average score of girls in HSC examination is 75 and that of boys is 70. The average score of all the candidates in the examination is 72. Find the ratio of number of girls and boys that appeared in the examination.

Answer :

Let total no. of boys be n_1 , total no. of girls be n_2 let the total number of students be 100.

$$\text{i.e. } n_1 + n_2 = 100$$

$$n_1 = 100 - n_2$$

from combined mean formula

$$n_1 = 100 - n_2 \quad \bar{x}_1 = 75 \quad \bar{x}_2 = 70$$

$$\bar{x} = \frac{n_1 \bar{x}_1 + n_2 \bar{x}_2}{n_1 + n_2}$$

$$72 = \frac{(100 - n_2) \times 75 + n_2 \times 70}{100}$$

$$72 \times 100 = 7,500 - 75n_2 + 70n_2$$

$$7,200 = 7,500 - 5n_2$$

$$-300 = -5n_2$$

$$n_2 = 60$$

$$\text{Then, } n_1 = 100 - 60 = 40$$

∴ the ratio of no. of girls and boys

$$= 40 : 60$$

$$= 2 : 3$$

Q.31 If $\frac{a+b}{a-b} = 2$, find the value of $\frac{a^2 - ab + b^2}{a^2 + ab + b^2}$.

Answer :

Given $(a+b) : (a-b) = 2:1$, we can write $a + b = 2$ and $a - b = 1$

$$a + b = 2$$

$$a - b = 1$$

$$2a = 3$$

$$a = \frac{3}{2}$$

$$a + b = 2$$

$$\frac{3}{2} + b = 2$$

$$b = 2 - \frac{3}{2} = \frac{1}{2}$$

$$\begin{aligned} \text{Value of } \frac{a^2 - ab + b^2}{a^2 + ab + b^2} &= \frac{\frac{9}{4} - \left(\frac{3}{2}\right) \left(\frac{1}{2}\right) + \frac{1}{4}}{\frac{9}{4} + \left(\frac{3}{2}\right) \left(\frac{1}{2}\right) + \left(\frac{1}{4}\right)} \\ &= \frac{9 - 3 + 1}{9 + 3 + 1} \\ &= 7 : 13 \end{aligned}$$

Q.32 What will be the cost price per kg of the mixture of two types of teas, mixed in the ratio 3:2 if the first type is purchased in ₹ 200 per kg and the second in ₹ 300 per kg.?

Answer :

Cost price per kg of the mixture

$$\begin{aligned} &= \frac{3 \times 200 + 2 \times 300}{3 + 2} \\ &= \frac{600 + 600}{5} \\ &= \frac{1200}{5} \\ &= 240 \end{aligned}$$

Q.33 If $\frac{x}{b+c} = \frac{y}{c+a} = \frac{z}{a+b}$, prove that

$$\frac{x(y-z)}{b^2-c^2} = \frac{y(z-x)}{c^2-a^2} = \frac{z(x-y)}{a^2-b^2}$$

Answer :

$$\text{Let } \frac{x}{b+c} = \frac{y}{c+a} = \frac{z}{a+b} = k$$

$$\text{then } x = (b+c)k, y = (c+a)k, z = (a+b)k$$

$$\begin{aligned} \frac{x(y-z)}{b^2-c^2} &= \frac{k(b+c)[(k(c+a) - k(a+b))]}{b^2-c^2} \\ &= \frac{(kb+kc)[kc+ka-ka-kb]}{b^2-c^2} \\ &= \frac{k^2(b+c)(c-b)}{b^2-c^2} \end{aligned}$$

$$\begin{aligned}
 &= \frac{c^2 - b^2}{b^2 - c^2} = -k^2 \\
 \frac{y(z-x)}{c^2 - a^2} &= \frac{(c+a)[k(a+b) - k(b-c)]}{c^2 - a^2} \\
 &= \frac{k(c+a)(ka + kb - kb - kc)}{c^2 - a^2} \\
 &= \frac{a^2 - c^2}{c^2 - a^2} = -k^2 \\
 \frac{z(x-y)}{a^2 - b^2} &= \frac{k(a+b)(kb + kc - kc - ka)}{a^2 - b^2} \\
 &= \frac{k^2(b^2 - a^2)}{a^2 - b^2} = -k^2
 \end{aligned}$$

$$\text{Hence, } \frac{x(y-z)}{b^2 - c^2} = \frac{y(z-x)}{c^2 - a^2} = \frac{z(x-y)}{a^2 - b^2} = -k^2$$

Proved

Q.34 Two vessels contain mixture of milk and water in the proportions 2:3 and 4:3 respectively. In what proportion should the two mixtures be mixed so as to form new mixture containing equal quantities of milk and water?

Answer :

Let x liter be drawn from vessel 1 and y liter from vessel 2

$$\begin{aligned}
 \frac{\frac{2}{5}x + \frac{4}{7}y}{\frac{3}{5}x + \frac{3}{7}y} &= \frac{1}{1} \\
 \frac{2}{5}x + \frac{4}{7}y &= \frac{3}{5}x + \frac{3}{7}y \\
 \frac{4}{7}y - \frac{3}{7}y &= \frac{3}{5}x - \frac{2}{5}x
 \end{aligned}$$

4.70**Solved Scanner CMA Foundation Paper - 4A (New)**

$$\frac{y}{7} = \frac{x}{5}$$

$$\therefore \frac{x}{y} = \frac{5}{7}$$

the two mixtures should be mixed in the ratio of 5 : 7.

Q.35 If 3, x and 27 are in continued proportion, find x.

Answer :

$$\frac{3}{x} = \frac{x}{27}$$

$$x^2 = 3 \times 27$$

$$x^2 = 81$$

$$x = 9$$

Q.36 What number is to be added to each term of the ratio 2 : 5 to make it 3 : 4 ?

Answer :

Let x be added to the ratio

$$\frac{2+x}{5+x} = \frac{3}{4}$$

$$8 + 4x = 15 + 3x$$

$$4x - 3x = 15 - 8$$

$$x = 7$$

Q.37 If the two numbers 20 and x + 2 are in the ratio 2 : 3, find x.

Answer :

$$\frac{20}{x+2} = \frac{2}{3}$$

$$60 = 2x + 4$$

$$60 - 4 = 2x$$

$$56 = 2x$$

$$x = \frac{56}{2} = 28$$

Q.38 If $\frac{\sqrt{a}-\sqrt{b}}{\sqrt{a}+\sqrt{b}} = \frac{1}{2}$, find the value of $\frac{a}{b}$.

Answer :

$$\sqrt{a} - \sqrt{b} = 1 \quad \dots\dots\dots(i)$$

$$\sqrt{a} + \sqrt{b} = 2 \quad \dots\dots\dots(ii)$$

$$\begin{array}{r} \hline 2\sqrt{a} = 3 \\ \sqrt{a} = \frac{3}{2} \end{array} \quad a = \frac{9}{4}$$

Putting the value of \sqrt{a} in eq. (i)

$$\frac{3}{2} - \sqrt{b} = 1$$

$$-\sqrt{b} = 1 - \frac{3}{2}$$

$$-\sqrt{b} = \frac{2-3}{2} = -\frac{1}{2}$$

$$\sqrt{b} = \frac{1}{2}, \quad b = \frac{1}{4}$$

$$\frac{a}{b} = \frac{\frac{9}{4}}{\frac{1}{4}} = \frac{9}{4} \times \frac{4}{1} = 9$$

Q.39 If $\frac{p}{b-c} = \frac{q}{c-a} = \frac{r}{a-b}$, prove that $p + q + r = 0 = pa + qb + rc$.

Answer :

$$p = k(b - c), q = k(c - a), r = k(a - b)$$

$$\text{L.H.S. } p + q + r = kb - kc + kc - ka + ka - kb = 0$$

$$\begin{aligned} \text{R.H.S } pa + qb + rc &= (b - c)a + (c - a)b + (a - b)c \\ &= ab - ac + bc - ab + ac - bc = 0 \end{aligned}$$

$$\therefore p + q + r = 0 = pa + qb + rc$$

Q.40 A dealer mixed two varieties of tea having costs ₹ 1,200 and ₹ 2,500 each per kg. in such a way that he can gain 20% by selling the resultant mixture at ₹ 1,800 per kg. Find the proportion in which the two types of tea are mixed.

4.72**Solved Scanner CMA Foundation Paper - 4A (New)****Answer :**Let the proportion of two types of tea mixed be $x : y$ then total cost of mixture = $1200x + 2500y$

resultant mixture is sold at 20% profit

$$\therefore (1200x + 2500y) \frac{120}{100} = 1800(x + y)$$

$$1200x + 2500y = 1500(x + y)$$

$$2500y - 1500y = 1500x - 1200x$$

$$1000y = 300x$$

$$10y = 3x$$

$$\frac{x}{y} = \frac{10}{3}$$

 \therefore the ratio of mixture = $10 : 3$.

Q.41 The banker's gain on a sum due 10 months hence at 6% per annum is ₹ 50. Find the sum due.

Answer :

$$BG = BD - TD$$

$$BD = A \times n \times i$$

$$TD = \frac{A \times i \times n}{n/12 + 1}$$

Where A = Sum due n = no. of years $BG = ₹ 50$ (given) r = rate per annum

$$BG = Ani - \frac{A}{n/12 + 1} \times i \times n$$

$$50 = \frac{A \times 10 \times 6}{12 \times 100} - \frac{A \times \frac{6}{100} \times \frac{10}{12}}{\left(\frac{10 \times 6}{12 \times 100} + 1\right)}$$

$$50 = \frac{A}{20} - \frac{A}{\left(\frac{1}{20} + 1\right)} \times \frac{1}{20}$$

$$50 = \frac{A}{20} - \left(1 - \frac{1}{\frac{1}{20} + 1} \right)$$

$$50 = \frac{A}{20} - \left(1 - \frac{20}{20 + 1} \right)$$

$$50 = \frac{A}{20} - \left(\frac{21 - 20}{21} \right)$$

$$50 = \frac{A}{420}$$

$$A = 420 \times 50 = ₹ 21,000$$

$$\text{Sum due} = ₹ 21,000$$

Q.42 A man borrowed ₹ 30,000 at 12% simple interest per annum from a bank. After 2 years, he paid ₹ 15,200 to the bank. Find how much he will have to pay after two years more to clear the loan.

Answer :

At first we need to find the amount he is required to pay after 2 years.

$$A = P [ni + 1] \quad \text{Where } n = 2, i = 12\% \quad P = ₹ 30,000$$

$$= 30,000 \left(\frac{2 \times 12}{100} + 1 \right)$$

$$= ₹ 37,200$$

∴ He is required to pay ₹ 37,200 of this the interest portion is 37,200 – 30,000 = ₹ 7,200. He pays ₹ 15,200. We assume that he pays ₹ 7,200 towards interest and balance amount towards principal, i.e. ₹ 8,000 (15,200 – 7,200)? the amount he is required to pay after two years to clear the loan.

$$P = 30,000 - 8,000 = ₹ 22,000$$

$$n = 2 \text{ years, } r = 12\%$$

$$A = P [ni + 1]$$

$$= 22,000 \left(\frac{2 \times 12}{100} + 1 \right)$$

$$= ₹ 27,280$$

Q.43 Find the present value of ₹ 4,000 due in 6 years if money is worth 5% compounded semi-annually.

Answer :

Given A = ₹ 4000 n = 6 years = 5%

Since interest is compounded semi-annually

$$n = 6 \times 2 = 12 \text{ half-yearly}$$

$$i = \frac{5}{2} = 2.5 \%$$

$$A = P (1 + i)^n$$

$$4,000 = P \left(1 + \frac{2.5}{100} \right)^{12}$$

$$4,000 = P (1.025)^{12}$$

$$\begin{aligned} \text{or, } P &= \frac{4,000}{(1.025)^{12}} \\ &= \frac{4,000}{1.34488} = ₹ 2,974 \end{aligned}$$

Q.44 Equal sum of money were lent to Omkar and Saurabh at 15% simple interest per annum for a period of 3 years and 4 years respectively. If the difference of interest paid by them was ₹ 300, find the sum lent.

Answer :

Simple Interest paid by Omkar = $p \times n \times r$

Where P = principal

r = rate of interest

n = no. of years

$$= P \times 3 \times \frac{15}{100} = 0.45 p$$

Simple interest paid by Saurabh = $p \times n \times r$

$$= p \times 4 \times \frac{15}{100} = 0.6 p$$

According to question

$$0.6 p - 0.45 p = 300$$

$$0.15 p = 300$$

$$P = \frac{300}{0.15} = ₹ 2,000$$

Q.45 Compute the Banker's Gain (B.G.) on a bill of ₹ 2,500 due in 6 months at 5% p.a.

Answer :

$$BG = BD - TD$$

$$BD = A \times n \times i, \quad TD = \frac{A}{(ni + 1)} \times i \times n$$

Where A = sum due

n = no. of years

i = rate per annum

$$A = ₹ 2,500 \quad n = 6 \text{ months} \quad r = 5 \%$$

$$\begin{aligned} BG &= A \times n \times i - \frac{A}{(ni + 1)} \times i \times n \\ &= 2,500 \times \frac{6}{12} \times \frac{5}{100} - 2, \frac{500}{\frac{6}{12} \times \frac{5}{100} + 1} \times \frac{5}{100} \times \frac{6}{12} \\ &= 62.5 - \frac{62.5}{1.025} \end{aligned}$$

$$= 62.5 - 60.9756 = ₹ 1.52 \text{ approx}$$

Q.46 A person has deposited ₹ 78,000 in Post Office Monthly Interest Scheme (MIS) after retirement at 8% p.a. Calculate his monthly income.

Answer :

$$P = ₹ 78,000$$

$$r = \frac{8\%}{12} = 0.6667 \%$$

$$T = 1 \text{ month}$$

$$S.I. = p \times r \times t$$

Where p = Principal

r = rate of interest

t = time

$$\begin{aligned} S.I. &= 78,000 \times 0.6667 \% \times 1 \\ &= ₹ 520 \text{ (approx)} \end{aligned}$$

4.76 ■ **Solved Scanner CMA Foundation Paper - 4A (New)**

Q.47 The population of a country increases every year by 2.4% of the population at the beginning of that year. In what time will the population double itself? Answer to the nearest year.

Answer :

Let population at the beginning of year be p
 $A = 2P$ $r = 2.4\%$
 $A = p(1 + i)^n$
 $A = p \left(1 + \frac{2.4}{100} \right)^n$ eq (i)
 $2p = p(1.024)^n$
 $2 = (1.024)^n$ (i)
 $n = 29.22$ years

Note : In eq (i) on keeping $n = 29$, we get value = 1.989 and on keeping $n = 30$ we get value = 2.037
 \therefore Difference = $(2.037 - 1.989) = 0.048$
 $0.048 \dots\dots\dots 12$
 $0.011 \dots\dots\dots \frac{12}{0.048} \times 0.011 = 2.75$
 on dividing $2.75 / 12 = 0.23$

Q.48 Calculate the interest on ₹ 10,000 for 10 years at 10% p.a.

Answer :

Simple interest is to be calculated in the question because it is not mention in the question that interest is compounded annually

Simple interest = $p \times n \times i$
 Where p = principal amount
 n = no. of years
 i = rate of interest
 $A = ₹ 10,000$ $n = 10$ years $r = 10\%$
 $S.I. = 10,000 \times 10 \times \frac{10}{100} = 10,000$

Q.49 A radio-dealer offers a radio for ₹ 270 cash down or ₹ 30 cash down and 18 equal monthly instalments of ₹ 15 each. Find the rate of simple interest charged.

Answer :

Cash price of radio = ₹ 270
 (-) down payment = ₹ 30
 Total installment payment = ₹ 240

Each installment of ₹ 15 is to be cleared in 18 months let the rate of simple interest to be charged be i

$$240 (1 + 18i) = 15 (1 + 17i) + 15 (1 + 16i) + 15 (1 + 15i) + \dots + (1 + 0i)$$

$$240 (1 + 18i) = 15 (18 + i (17 + 16 + 15 + \dots + 0))$$

$$240 (1 + 18i) = 15 (18 + i \times 153)$$

$$240 + 4,320i = 270 + 2295i$$

$$4,320i - 2,295i = 270 - 240$$

$$2,025i = 30$$

$$i = \frac{30}{2025} = 0.0148$$

$$\therefore \text{yearly interest rate, } i = 0.0148 \times 12 = 0.17777$$

$$\therefore \text{rate of simple interest charged} = 17.77\%$$

Q.50 The true discount (TD) on a bill for ₹ 2,160 due sometime hence is ₹ 180; find the Banker's gain (BG) on the same bill at the same rate.

Answer :

$$TD = \frac{Ani}{(ni+1)} \quad BD = A \times n \times i$$

$$BG = BD - TD$$

Where = TD = True Discount

BD = Bankers Discount

A = Bill Amount

n = rate of interest

BG = Bankers gain

$$\text{Given TD} = 180 \quad A = ₹ 2,160$$

$$\text{i.e.} \quad \frac{Ani}{(ni+1)} = 180$$

$$\frac{2160 \times ni}{ni+1} = 180$$

$$2,160 \times ni = 180ni + 180$$

4.78**Solved Scanner CMA Foundation Paper - 4A (New)**

$$2,160 ni - 180 ni = 180$$

$$1980 ni = 180$$

$$ni = \frac{180}{1980} = 0.0909$$

$$\begin{aligned} BD &= A \times n \times i \\ &= 2,160 \times 0.0909 = 196.36 \end{aligned}$$

$$\begin{aligned} \therefore BG &= BD - TD \\ &= 196.36 - 180 \\ &= ₹ 16.36 \end{aligned}$$

Q.51 A sum of money becomes double in 20 years at simple interest. Find the number of years by which the sum will be triple.

Answer :

Let sum of money be ₹ P money gets double in 20 years

$$A = (P) (ni + i)$$

$$2(P) = (P) (ni + 1)$$

$$2P = P (20i + 1)$$

$$2 = 20i + 1$$

$$2 - 1 = 20i$$

$$\frac{1}{20} = i$$

$$i = \frac{1}{20} \times 100 = 5\%$$

No. of years in which money gets triple

$$A = (P) (ni + 1)$$

$$3(P) = (P) \left(n \times \frac{5}{100} + 1 \right)$$

$$3 = \frac{5n}{100} + 1$$

$$3 = \frac{5n+100}{100}$$

$$300 = 5n + 100$$

$$300 - 100 = 5n$$

$$200 = 5n$$

$$n = \frac{200}{5} = 40 \text{ years}$$

Q.52 The simple interest on ₹ 300 at the rate of 4% per annum with that on ₹ 500 at the rate of 3% per annum, both for the same period, is ₹ 162. Find the time period.

Answer :

Let the time period be n

$$\text{S.I.} = p \times n \times i$$

p = principal S.I.= Simple interest

i = rate of interest

n = no. of years

$$\text{S.I. at 4\% p.a.} = 300 \times \frac{4}{100} \times n = 12n$$

$$\text{S.I. at 3\% p.a.} = 500 \times \frac{3}{100} \times n = 15n$$

According to question

$$12n + 15n = 162$$

$$27n = 162$$

$$n = \frac{162}{27} = 6$$

Q.53 At what simple interest rate percent per annum a sum of money will be doubled of itself in 25 years?

Answer :

Let the sum of money be ₹ p

$$A = p (ni + 1)$$

$$A = 2p = p (25i + 1)$$

$$2p = p (25i + 1)$$

$$2 = 25i + 1$$

$$2 - 1 = 25i$$

$$1 = 25i$$

$$i = \frac{1}{25}$$

$$i = \frac{1 \times 100}{25} = 4\%$$

Q.54 At what rate per annum will a sum of money double itself in 10 years with simple interest?

Answer :

Let the sum of money be ₹ p

$$A = p (ni + 1)$$

$$A = 2 p \quad n = 10$$

$$2 p = p (10 i + 1)$$

$$2 = 10 i + 1$$

$$2 - 1 = 10 i$$

$$1 = 10 i$$

$$i = \frac{1 \times 100}{10} = 10 \%$$

Q.55 At the same rate of simple interest a principal amounts to ₹ 2,056 in 4 years and amounts to ₹ 2,248 in 7 years. Find the rate of interest and the principal.

Answer :

$$A = p (ni + 1)$$

$$2056 = p (4 \times i + 1) \quad \dots\dots\dots(i)$$

$$2248 = p (7 \times i + 1) \quad \dots\dots\dots(ii)$$

Dividing eq (ii) by eq (i)

$$\frac{2248}{2056} = \frac{p(7i+1)}{p(4i+1)}$$

$$2,248 (4 i + 1) = 2,056 (7 i + 1)$$

$$8,992 i + 2,248 = 14,392 i + 2,056$$

$$2,248 - 2,056 = 14,392 i - 8,992 i$$

$$192 = 5,400 i$$

$$i = \frac{192}{5,400} = 0.035555$$

$$\text{or, } i = 0.035555 \times 100 = 3.55 \%$$

Putting value of i in eq (i)

$$2,056 = p (4 \times 0.0355 + 1)$$

$$2,056 = p (0.142 + 1)$$

$$2,056 = p (1.142 + 1)$$

$$2,056 = p (1.142)$$

$$p = \frac{2,056}{1.142} = ₹ 1,800$$

Q.56 What principal will be increased to ₹ 4,600 after 3 years at the rate of 5% per annum simple interest ?

Answer :

$$A = p (n i + 1)$$

$$A = ₹ 4,600 \quad n = 3 \text{ yrs} \quad r = 5 \%$$

$$4,600 = p (3 \times 0.05 + 1)$$

$$4,600 = p (1.15)$$

$$p = \frac{4,600}{1.15} = ₹ 4,000$$

Q.57 An engine without any wagons can run 24 km/hr and its speed is diminished by a quantity varying as the square root of the number of wagons attached to it. With 4 wagons its speed becomes 20 km/hr. Find the maximum number of wagons with which the engine can move.

Answer :

Let n be the no. of wagons

$$\text{Now speed} = 24 - k \sqrt{n}$$

Where k = a constant

$$\text{Again} \quad 20 = 24 - k \sqrt{n} \quad (\text{According to Question})$$

$$20 - 24 = -k \sqrt{4}$$

$$4 = k \sqrt{4} \text{ or, } 4 = 2k$$

$$K = \frac{4}{2} = 2$$

Maximum wagon to be attached so that engine cannot move, i.e. Speed = 0

$$0 = 24 - 2\sqrt{n}$$

$$2\sqrt{n} = 24$$

$$\sqrt{n} = \frac{24}{2} = 12, \text{ or } n = 144$$

∴ When 144 wagons are attached, engine cannot move.

So, maximum number of wagons with which the engine can move = 144-1 = 143 wagons.

Q.58 If a varies as b prove that $a + b$ varies as $a - b$.

Answer :

Given a varies b

i.e. $a = kb$, where $k =$ a constant

To prove: $a + b$ varies as $a - b$

i.e. $\frac{a+b}{a-b} =$ a constant [as per variation rule]

L.H.S

$$\frac{a+b}{a-b} = \frac{kb+b}{kb-b} \text{ [putting value of } a]$$

$$= \frac{b(k+1)}{b(k-1)} = \text{a constant}$$

\therefore L.H.S = R.H.S

$\therefore a + b$ varies as $a - b$

Q.59 If $a + 2b$ varies as $a - 2b$, prove that a varies as b .

Answer :

$a+2b$ varies as $a-2b$

i.e. $\frac{a+2b}{a-2b} =$ a constant = k (let)

To prove :- a varies as b

i.e. $\frac{a}{b} =$ a constant [as per variation rule]

$$\text{L.H.S } \frac{a+2b}{a-2b} = k$$

$$a + 2b = k(a - 2b) \text{ [on cross multiplication]}$$

$$a + 2b = ak - 2bk$$

$$a - ak = -2bk - 2b$$

$$a(1 - k) = -2b(k+1)$$

$$+ a(k-1) = + 2b(k+1)$$

$$\frac{a}{b} = \frac{2(k+1)}{(k-1)} = \text{a constant}$$

$$\therefore \text{L.H.S} = \text{R.H.S}$$

a varies as b

Q.60 As the number of units manufactured in a factory is increased from 200 to 300, the total cost of production increases from ₹16,000 to ₹ 20,000. If the total cost of production is partly fixed and other part varies as number of units produced, find the total cost for producing 500 units.

Answer :

Let the total cost function be

$$Y = a + bx$$

Where

Y = total cost

X = no. of units.

a,b are constants.

Total Cost	production units
16,000	200
20,000	300

By using above information, we get following equations:

$$16,000 = a + 200b \text{ ----- (i)}$$

$$20,000 = a + 300b \text{ ----- (ii)}$$

Solving eq(i) and eq(ii) simultaneously

$$a + 200b = 16,000$$

$$a + 300b = 20,000$$

$$\begin{array}{r} (-) \quad (-) \quad (-) \\ \hline \end{array}$$

$$+100b = + 4000$$

$$b = \frac{4000}{100} = 40$$

Putting value of b in eq (i)

$$16,000 = a + 200 \times 40$$

$$a = 16,000 - 8,000$$

$$a = 8,000$$

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∴ Total cost function is given by

$$y = 8,000 + 40x$$

Hence, Total cost of producing 500 units

$$y = 8,000 + 40 \times 500$$

$$= ₹ 28,000$$

Q.61 If $(a + b)$ varies as $(a - b)$, prove that $a^2 + b^2$ varies as b^2 .

Answer :

Given $a + b$ varies as $a - b$

$$\text{i.e. } \frac{a+b}{a-b} = \text{a constant [As per variation rule]}$$

To prove: $a^2 + b^2$ varies as b^2

$$\text{i.e. } \frac{a^2+b^2}{b^2} = \text{a constant}$$

$$\text{Proof: } \frac{a+b}{a-b} = k \text{ (let)}$$

$$a + b = ka - kb$$

$$a - ka = -kb - b$$

$$a(1 - k) = -b(k + 1)$$

$$+ a(k - 1) = +b(k + 1)$$

$$a(k - 1) = b(k + 1)$$

$$\frac{a}{b} = \frac{k+1}{k-1} = \text{a constant}$$

$$\text{Now } \frac{a}{b} = m \text{ (let)}$$

$$\text{or, } a = bm$$

$$\text{L.H.S. : } \frac{a^2+b^2}{b^2} = \frac{(bm)^2+b^2}{b^2}$$

$$= m^2 + 1 = \text{a constant}$$

$$\therefore \text{L.H.S} = \text{R.H.S}$$

$$\therefore a^2 + b^2 \text{ varies as } b^2$$

Q.62 The expenses of a boarding house are partly fixed and partly varies with the number of boarders. The charge is ₹ 70 per head when there are 20 boarders and ₹ 60 per head when there are 40 boarders. Find the charge per head when there are 50 boarders.

Answer :

Let total charge function for boarders = $y = a + bx$

Where y = cost function

x = no. of boarders

And, a = fixed cost and b = variable cost

According to Question

$$20 \times 70 = a + b \times 20 \text{----- (i)}$$

$$40 \times 60 = a + b \times 40 \text{----- (ii)}$$

Solving eq(i) and (ii) simultaneously

$$a + 20b = 1400$$

$$a + 40b = 2400$$

$$\begin{array}{r} (-) \quad (-) \quad (-) \\ \hline \end{array}$$

$$- 20b = - 1,000$$

$$b = 50$$

Putting value of b in eq (i)

$$70 \times 20 = a + 20 \times 50$$

$$1400 = a + 1000$$

$$a = 1400 - 1000$$

$$= 400$$

$$\therefore \text{Total cost function} = 400 + 50x$$

Total cost for 50 boarders

$$= 400 + 50 \times 50$$

[putting value of $x = 50$ in total cost function 50 ascertain]

$$= 400 + 2500$$

$$= ₹ 2,900$$

Charge per head for 50 boarders

$$= \frac{2900}{50} = ₹ 58 \text{ per head}$$

4.86**Solved Scanner CMA Foundation Paper - 4A (New)**

Q.63 If x varies as y then show that $x^2 + y^2$ varies as $x^2 - y^2$.

Answer :

Given: x varies as y

$$\text{i.e. } \frac{x}{y} = \text{a constant [As per variation rule]}$$

To prove: $x^2 + y^2$ varies as $x^2 - y^2$

$$\text{i.e. } \frac{x^2 + y^2}{x^2 - y^2} = \text{a constant}$$

$$\text{L.H.S: } \frac{x}{y} = k \text{ (let)}$$

$$x = ky$$

$$\frac{x^2 + y^2}{x^2 - y^2} = \frac{(ky)^2 + y^2}{(ky)^2 - y^2} = \frac{y^2(k^2 + 1)}{y^2(k^2 - 1)} = \text{a constant}$$

\therefore L.H.S = R.H.S

$x^2 + y^2$ varies as $x^2 - y^2$